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Intelligent Intrusion Detection Using Radial Basis Function Neural Network

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Abstract— Recently we witness a booming and ubiquity evolving of internet connectivity all over the world leading to dramatic amount of network activities and large amount of data and information transfer. Massive data transfer composes a fertile ground to hackers and intruders to launch cyber-attacks and various types of penetrations. As a consequence, researchers around the globe have devoted a large room for researches that can handle different types of attacks efficiently through building various types of intrusion detection systems capable to handle different types of attacks, known and unknown (novel) ones as well as have the capability to deal with large amount of traffic and data transferring. In this paper, we present an intelligent intrusion detection system based on radial basis function capable to handle all types of attacks and intrusions with high detection accuracy and precision through addressing the intrusion detection problem in the framework of interpolation and adaptive network theories.

Index Terms— artificial neural network, data approximation, clustering, interpolation, intrusion detection, radial basis function.

I. INTRODUCTION

Data encryption, user authentication and firewalls are most common classical regimes for computer network protection. However, as conducting network cyber activities is in increasing pattern with tendency to high levels of breaches and penetration, the classical protection techniques collapsed in front of these attacks. The situation gets harder if the target organizations and establishments are of highly sensitive data containers such as: banks, telecom, and military agents. Intelligent software intrusion detection systems represent the typical solution for cases cannot be handled by classical security techniques. This is due to the learning capability in one hand and due to adaptivity shown by these systems on the other hand. Most of intelligent intrusion detection systems are built using Artificial Intelligence (AI) such as swarm intelligence, case-based reasoning, neural networks and fuzzy logic, rule-

based systems, cellular automata, reinforcement learning, multi-agent systems, and hybrid systems built by hybrid of two or more of these techniques. Artificial neural networks are used extensively to model the nonlinear mapping of intrusion detection problem. Radial Basis Function (RBF) neural network represents a typical type of powerful neural networks that show high capability in binary and class-wise classification problems including intrusion detection.

As an early implementations of basic RBF Network (RBFN) for sake of security and intrusion detection are that proposed by Yang *et al.* [1], Jing *et al.* [2] and Devaraju and Ramakrishnan [3]. Rapaka *et al.* [4] used the classical version of RBF network for combining misuse and anomaly detections. Exploiting the short training time acquired by RBFNN, Jiang *et al.* [5] proposed a hierarchical intrusion detection system composed of multiple layers of RBFN structured in parallel and serial manners for real-time implementation.

On the other hand, for optimized RBF mapping operation, Particle Swarm Optimization (PSO) was used by Chen *et al.* [6] to enhance RBFN parameters in sake of solving issues such as poor generalization and low detection sensitivity. Xu *et al.* [7] used hybrid of PSO technique and kernel principal component analysis to extract the core nonlinear characteristic of dataset whereas Other researchers [8] adapted genetic algorithm-chaos as RBFNN optimization technique.

Instead of using classical clustering techniques such as k-means and Self-Organized Map (SOM) to search for candidate RBFN hidden neurons, Zhong *et al.* [9] employed a multiple granularities immune neural network algorithm for constructing the hidden layer of RBFN whereas Yichun *et al.* [10] used immune recognition algorithm as RBFN learning algorithm. For detecting new attacks in continual manner, Tian *et al.* [11] integrate SOM network to generate new nodes in RBF network for on-line intrusion detection. Other intrusion detection structures were built based on a hybrid combination of RBFN and other techniques to enhance the overall performance of

intrusion detection. Ma *et al.* [12] proposed a hybrid learning algorithm for RBFN based on combination of Quantum-Behaved Particle Swarm Optimization (QPSO) and gradient descent algorithm. As another example of hybrid techniques, a hybrid scheme was presented by Li-Zhong *et al.* [13] for intrusion detection composed of rough set and RBFN. Most of aforementioned literature addressed the problem of intrusion detection as a sort of nonlinear mapping problem. In our work, we addressed the intrusion detection from pure mathematical perspective leading to high detection performance without the need for complicated hybrid schemes and preliminary stages for RBF parameters optimization.

We first introduce the problem of intrusion detection in the framework of mathematical approximation (interpolation) and introduce our intrusion detection system in Section II. We show our results associated with comparisons and discussion in Section III. Section IV concludes the paper.

II. RADIAL BASIS FUNCTION AS INTRUSION DETECTION TECHNIQUE

In this section, we formulate the problem of intrusion detection in a pure mathematical framework ending up with intrusion detection system as a sort of adaptive network.

A. RBF as Strict Interpolator (Approximator)

As a concept, radial basis function has its root in approximation theory of mathematics, in particular, in the field of strict multivariate functions interpolation where the treated problem is: Consider a set of \mathcal{M} distinct data items (vectors) as $\{x_i; i = 1, 2, \dots, \mathcal{M}\}$ in \mathfrak{R}^d and a set of \aleph real numbers $\{f_i; i = 1, 2, \dots, \aleph\}$ in \mathfrak{R} in such a way, we choose a function (mapping)

$U: \mathfrak{R}^d \rightarrow \mathfrak{R}$ which satisfies the strict interpolation condition as in (1):

$$U(x_i) = f_i, \quad i = 1, 2, \dots, \mathcal{M} \quad (1)$$

It is worth noting that $U(x_i)$ is constrained to go through all available data points.

The core idea of radial basis function is to establish a linear space of functions. The basis functions of this space depend on the “radial” distance between the data items and the centers of these functions. For sake of constructing the space, a set of \mathcal{M} basis functions $\varphi(\|x_i - x^c\|)$ is used, where, in general, $\varphi(\cdot)$ is nonlinear of distance between data item x_i and centers of basis functions x^c .

In order to approximate a function, a linear combination of these $\varphi(\cdot)$ functions used as in (2):

$$U(x_i) = \sum_{j=1}^{\mathcal{M}} \lambda_j \varphi(\|x - x_j^c\|) \stackrel{\text{def}}{=} \sum_{j=1}^{\mathcal{M}} \lambda_j \varphi_j(r) \quad (2)$$

Referring to (1), $U(x_i) = f_i$, Therefore,

$$f_i = \sum_{j=1}^{\mathcal{M}} \lambda_j \varphi_j(r) \quad (3)$$

In terms of matrices, equation (3) can be re-written as in (4):

$$\begin{pmatrix} f_1 \\ f_2 \\ \vdots \\ f_{\aleph} \end{pmatrix} = \begin{pmatrix} A_{11} & \dots & A_{\mathcal{M}1} \\ \vdots & \dots & \vdots \\ A_{\mathcal{M}1} & \dots & A_{\mathcal{M}\mathcal{M}} \end{pmatrix} \begin{pmatrix} \lambda_1 \\ \lambda_2 \\ \vdots \\ \lambda_{\aleph} \end{pmatrix} \quad (4)$$

Where

$$A_{ji} = \varphi(\|x - x_j^c\|) \quad (5)$$

Thus, if A_{ji}^{-1} exist, then $U(x_i)$ can be *strictly* approximated using (6):

$$\lambda = A^{-1} \mathbf{f} \quad (6)$$

Where λ and \mathbf{f} are vectors.

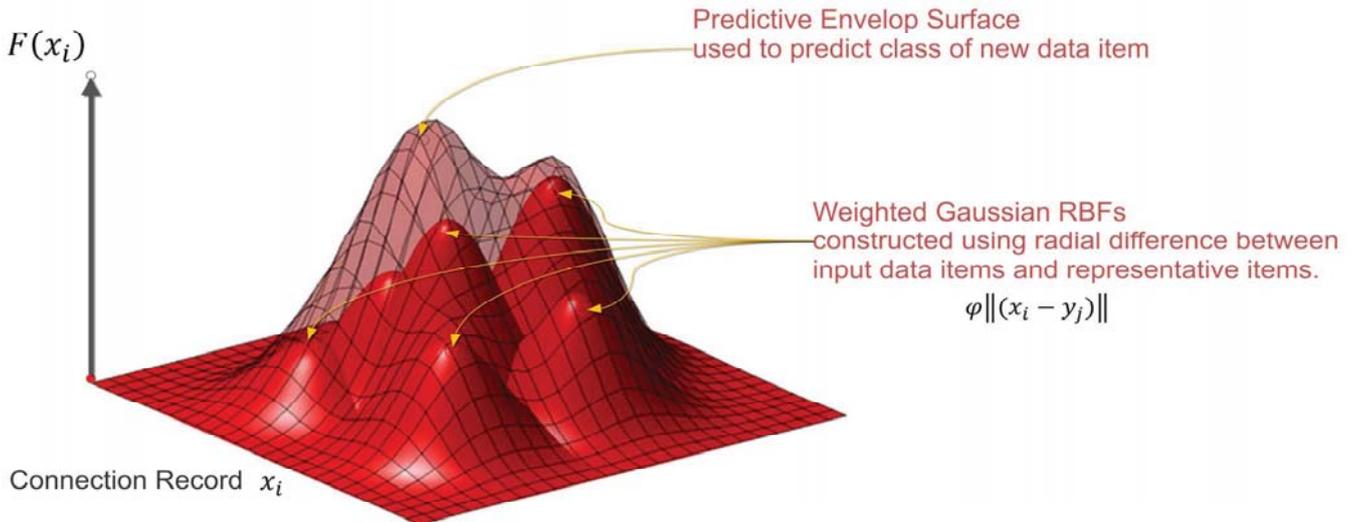


Fig. 1. Explanatory example of predictive surface generated by six weighted and spatially shifted Gaussian bells in 2D space produced by means of RBF neurons [14]. Note that $x_i \in \mathfrak{R}^2$ instead of \mathfrak{R}^d , for purpose of clarification.

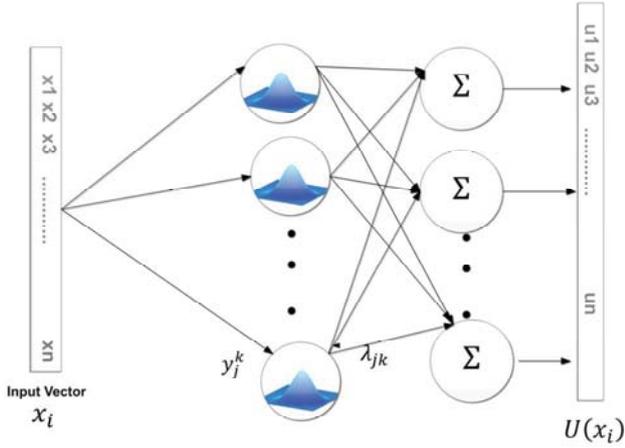


Fig. 3. Graphical representation of (9) where $U: \mathfrak{R}^{41} \rightarrow \mathfrak{R}^n$

$$U(x_i) = \lambda_{ok} + \sum_{j=1}^M \lambda_{jk} \varphi(\|x_i - y_j^k\|) \quad (9)$$

where
 $x_i \in \mathfrak{R}^d$, $U \in \mathfrak{R}^n$ j : number of cluster centers, $j = 1, 2, \dots, N_0$ $k = 1, 2, \dots, n$. Since our input vector is of high independent components $x_i \in \mathfrak{R}^{41}$, λ_{ok} represents the constant offset (bias) for each k^{th} component of U vector. which can be depicted as in Fig. 3.

The binarization of (9) takes the form as in (10):

$$u_k = \begin{cases} 1, & \text{if } u_k = \max_k\{U\} \\ 0, & \text{otherwise} \end{cases} \quad (10)$$

Therefore, the type of attack can be identified through scoring process of the sum's outputs of (9), i.e., the sum of high score (cumulative output) give rise to a specific attack type.

III. EXPERIMENTAL ANALYSIS AND RESULTS

In this section, RBF-based intrusion detection system is

applied to NSL-KDD dataset for sake of multi-classification. The proposed work was implemented on MATLAB 2018b, working on a system with an i7 processor having 8GB RAM. In this application, we adapt two-phase RBF training through k-means algorithm of $k = 15$, where σ 's and μ 's values of the clusters were found and used to establish Gaussian functions φ 's of hidden neurons as illustrated in Fig. 4. In this work, we designed a multi-class intrusion detection scheme, namely, instead of detecting normal or attack, the system can detect the attack and classify the type that belongs to as shown in Table I.

TABLE I
 ATTACK CATEGORIES AND SUB-CATEGORIES FOUND IN TRAINING AND TESTING DATASETS

DOS	Probe	R2L	U2R
Back	Satan	Guess_password	Buffer-overflow
Land	Ipsweep	Guess-passwd	Loadmodule
Neptune	Nmap	ftp-write	Rootkit
Pod	Portsweep	Imap	Perl
Smurf	Mscan	Phf	Sqlattack
Teardrop	Saint	Multihop	Xterm
Mailbomb		Waremaster	Ps
Processtable		Xlock	
Udpstorm		Xsnoop	
Apache2		Smppguess	
Worm		Smppgetattack	
		Httpunnel	
		Sendmail	
		Named	
		Warezclient	
		Spy	

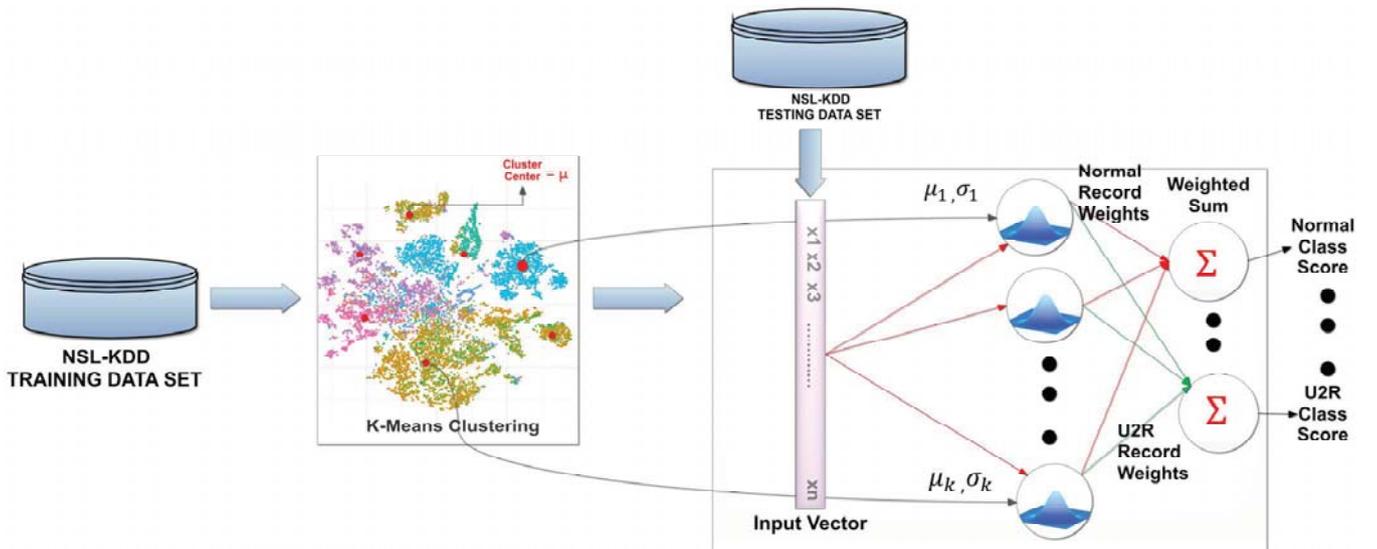


Fig. 4. Graphical pipeline of experimental analysis of proposed RBF-based IDS.

NSL-KDD dataset shows high levels of imbalance between different attacks statistics, for example, the low frequency of U2R and R2L instances in contrast to high frequency of DOS and Probe instances leads to explicit biasing of detection performance towards high frequent classes. Moreover, this imbalance lessens the sensitivity of RBF functions towards low frequent attacks which lowers the detection performance reliability.

As a pre-liminary data pre-processing step, we followed same steps were conducted in [17] except one *core* step impacts our detection performance. In this work, we address the issue of data imbalance by oversampling least frequent instances {U2R, R2L} leading to increase the total statistics of these types of attacks increasing the number of total records that involved in the testing and training phases of proposed model which ends up with a new statistic for our datasets.

The attack label is classified into one of four categories:

DOS: Denial of Service Attacker attempts to not allowing legitimate users from using a service.

Prob: Probing Attacker attempts to discover vulnerable hosts in the internet.

R2L: Remote to Local

Attacker does not have an authorized local access and attempts to gain unauthorized one.

U2R: User to Remote

Attacker have an authorized local access, but attempts to grab the privilege of root (administrator) access.

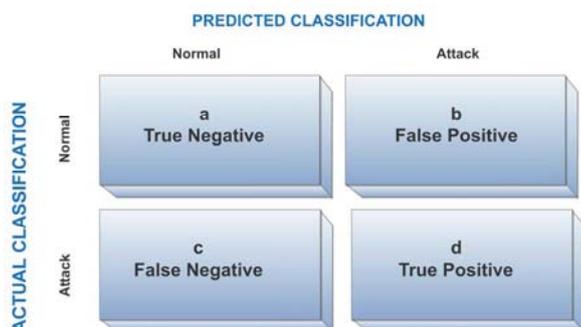


Fig. 5. Confusion matrix of detection response.

Each of attack categories include several attack types as illustrated in Table I. As a final step of preliminary dataset processing, according to Table I, labels of connection records undergo discretization where the different types of attacks grouped into one category and given discrete integer value: {Normal:0, DOS: 1, Probe: 2, R2L:3, U2R: 4}, which, in other hand, represent distinct values of f_i .

In this work, we adopted two types of overall performance evaluation: (1) Binary-wise performance evaluation. (2) Class-wise overall performance evaluation. Where the former is built on binary confusion matrix of intrusion detection outputs, whereas the later is built based on the class-wise confusion matrix where the average of multi-class system responses is calculated and considered as overall performance. Both types of performance evaluation use same measures that are

essentially based on the confusion matrix as elaborated in Fig. 5. Based on Fig. 5, the classification results of testing connection records are typically given in terms of the following measures of performance (11- 14):

$$\text{Sensitivity(Detection Rate)} = \frac{d}{(d+c)} \quad (11)$$

$$\text{False Positive Rate (FPR)} = \frac{b}{(b+a)} \quad (12)$$

$$\text{Positive Predictive Value(Precision)} = \frac{d}{(d+b)} \quad (13)$$

$$\text{Accuracy (Acc)} = \frac{d+a}{(a+b+c+d)} \quad (14)$$

TABLE II
BINARY-WISE CONFUSION MATRIX

PREDICTED		
	Normal	Attack
ACTUAL		
Normal	19793	551
Attack	1136	18521

TABLE III
CLASS-WISE CONFUSION MATRIX

PREDICTED					
ACTUAL	Normal	DoS	Probe	R2L	U2R
Normal	19793	170	126	252	3
DoS	492	13269	90	4	0
Probe	252	127	3067	0	0
R2L	382	0	0	1695	2
U2R	10	0	0	15	252

Using subset of 40,000 records for sake of performance testing and validation and 15 neurons for the hidden layer of RBFNN, simulation results of our intrusion detection system are given as confusion matrix of attack detection in type and the corresponding performance metrics as shown in Table II and Table III respectively.

In this paper, our proposed model is compared with two prominent types of RBF-based intrusion detection systems: (1) Intrusion detection systems built on classical version of RBF as listed in Table V. (2) Intrusion detection systems built on optimized (improved) version of RBF or systems built using RBF network as a part of a hybrid intrusion detection system as listed in TABLE VI. The first type (which our proposed model belongs to) employs the basic version of RBF network to classify the records using simple clustering technique (as k-means or SOM) to set network parameters.

TABLE V
COMPARATIVE ANALYSIS WITH CLASSICAL RBF NETWORK BASED ID SYSTEMS/MODELS

Method	Accuracy	Detection Rate	FP	Precision	Response Time
Rapaka <i>et al.</i> [4]	97%	-	-	-	-
Jiang <i>et al.</i> [5]	-	Single-Layer RBF-IDS: DoS : 98.4% Probe : 99.6% R2L : 98.0%	Single-Layer RBF-IDS: DoS : 0% Probe: 0% R2L : 0%	-	3 min / 4,900,000 training records
Jiang <i>et al.</i> [5]	-	Multi-Layered RBF-IDS: SHIDS ^a : Normal: 99.5% Ipsweep 99.1% Smurf: 99.3% Guess-Pass: 98.2% Buffer-Over: 94.1%	Multi-Layered RBF-IDS: SHIDS: Normal: 1.2% Ipsweep 1.62% Smurf: 4.5% Guess-Pass: 0% Buffer-Over: 5.4%	-	-
		PHIDS ^b : Normal: 99.8% Ipsweep 99.5% Smurf: 99.0% Guess-Pass: 99.7% Buffer-Over: 98.8% PortswEEP: 86.9%	PHIDS: Normal: 1.2% Ipsweep 0.8% Smurf: 0% Guess-Pass: 4% Buffer-Over: 3.3% PortswEEP: 0%		
Yang <i>et al.</i> [1]	-	97.1%	1.6%	-	4 sec / 1,200 training records
Bi <i>et al.</i> [2]	-	87%	-	-	-
Devaraju and Ramakrishnan [3]	75.4% (400 test records)	-	-	-	-
Shi <i>et al.</i> [8]	-	77.6%	3.27%	-	-
Chen <i>et al.</i> [6]	Class-wise: DoS : 85.14% Probe : 81.71% R2L : 88.00% U2R : 86.86%				
Li-Zhong <i>et al.</i> [13]	83.5% (1190 testing records) 82.5% (2170 testing record)	-	-	-	-
Proposed RBFN IDS	Class-wise: DoS : 98.04% Probe : 98.37% R2L : 97.13% U2R : 99.94% Average: 98.37%	Class-wise: DoS : 96.42% Probe : 92.41% R2L : 81.61% U2R : 96.18% Average: 92.86%	Class-wise: DoS : 0.85% Probe : 0.63% R2L : 1.26% U2R : 0.015% Average: 0.688%	Class-wise: DoS : 98.74% Probe : 96.05% R2L : 87.06% U2R : 98.82% Average: 95.16%	7.11 sec/ 68,000 training records 3.39 sec/ 40,000 testing records
	Binary-wise: 95.87%	Binary-wise: 94.22%	Binary-wise: 2.7%	Binary-wise: 97.11%	

^aSHIDS Serial Hierarchical RBF-IDS.^bPHIDS Parallel Hierarchical RBF-IDS.

On the other hand, the optimized versions of RBF network use optimization techniques to determine the optimal values of these parameters or combine the classical RBF network with other classification technique in a hybrid manner. In our proposed model, instead of optimizing RBF network, we optimized the training dataset that used to determine the parameters of Gaussian functions, we established a balanced grid of high selective Gaussian functions for each type of attacks leading to a balanced bank of filters which, reflect in high detection performance without optimization or hybrid

steps. Based on the detection results provided in Table II and Table III the binary and class-wise overall performance evaluation represented by detection accuracy, detection rate, false positive rate, precision and time responses for training and testing stages of our proposed system associated with a comparison to other classical, optimized and hybrid RBFN-based intrusion detection models/systems are presented in Table V and Table VI respectively. Examining the results provided in Table V, it can be observed that although our proposed classifier uses the classical version of RBF network

TABLE VI
COMPARATIVE ANALYSIS WITH OPTIMIZED/HYBRID RBF NETWORK BASED ID SYSTEMS/MODELS

Method	Accuracy	Detection Rate	FP	Precision	Response Time
Zhong <i>et al.</i> [9]	-	94.04%	0.71%	-	-
Yichun <i>et al.</i> [10]	-	-	-	83.7%	-
Xu <i>et al.</i> [7]	-	Class-wise: Normal: 84.14% DoS : 100 % Probe : 48% R2L : 81.6% U2R : 42%	Class-wise: Normal: 1.28% DoS : 0 % Probe : 30% R2L : 0.45% U2R : 30.3%	-	-
		Binary-wise: 98.95%	Binary-wise: 2.05%		
Shi <i>et al.</i> [8]	-	Class-wise: DoS : 97.6% Probe : 96.3% R2L : 98.1% U2R : 95.4%	Class-wise: DoS : 0.92% Probe : 0.83% R2L : 0.99% U2R : 0.86%	-	-
		Binary-wise: GA-RBF: 86.8% Chaos-GA-RBF: 95.4%	Binary-wise: GA-RBF: 1.21% Chaos-GA-RBF: 1.05%		
Chen <i>et al.</i> [6]	Class-wise: DoS : 92.57% Probe : 88.86% R2L : 94.29% U2R : 91.57%	-	-	-	-
Ma <i>et al.</i> [12]	-	QPSO-RBFN 92.08%	QPSO-RBFN 5.29%	-	-
Li-Zhong <i>et al.</i> [13]	92.8% (1190 testing records) 91% (2170 testing record)	-	-	-	-
Proposed RBFN IDS	Class-wise: DoS : 98.04% Probe : 98.37% R2L : 97.13% U2R : 99.94% Average: 98.37%	Class-wise: DoS : 96.42% Probe : 92.41% R2L : 81.61% U2R : 96.18% Average: 92.86%	Class-wise: DoS : 0.85% Probe : 0.63% R2L : 1.26% U2R : 0.015% Average: 0.688%	Class-wise: DoS : 98.74% Probe : 96.05% R2L : 87.06% U2R : 98.82% Average: 95.16%	7.11 sec/ 68,000 training records 3.39 sec/ 40,000 testing records
	Binary-wise: 95.87%	Binary-wise: 94.22%	Binary-wise: 2.7%	Binary-wise: 97.11%	

as the principal classifier, it has achieved high detection performance, where 40,000 records take about less than 4 seconds to be tested and less than 8 seconds to build the system model using 65,000 training records. Moreover, the system shows high accuracy towards rare attacks {R2L and U2R} reached up to 97.13% and 99.94% and FPR as low as 1% and 0.015% for R2L and U2R respectively. Referring to Table V, among all classical RBF-based IDS systems, our proposed model achieved the best in terms of class-wise accuracy and it is competitive with other systems and is particularly strong in all performance measures when dealing with rare and difficult-to-detect U2R attacks.

In terms of detection rate, our proposed model falls behind some other methods such as proposed by Jiang *et al.* [5] and Yang *et al.* [1]. However, for single layer IDS proposed by [5], the system can detect all types of attacks *except* U2R attack. Moreover, in case of multi-layered IDS proposed by same authors, the system was designed to deal with very specific types of major types of attacks, i.e., referring to TABLE I, Ipsweep belongs to Probe attack category, smurf belongs to DoS, Guess-pass belongs to R2L and buffer-overflow belongs to U2R category. In contrast, our proposed system has the ability to deal with a broad band of attack types per each attack category with competitive class-wise detection rates, precisions and FPRs and without the complexity of multi-layered structures. Moreover, both references [5] and [1] used KDD Cup'99 dataset for testing, training and validation purposes whereas, our proposed system was trained, tested and validated using NSL-KDD dataset which is considered a challenging dataset especially for multi-class wise intrusion detection. Interestingly, according to recent survey done by Chowdhury *et al.* [18], it was found that detection accuracy of intrusion detection systems built using NSL-KDD dataset was stuck around 85% approximately for multi-class classifiers that used all features. On the contrary, most of intrusion detection systems were built using KDD Cup'99 had achieved impeccable detection performance reached up to 100% for some schemes; especially for binary classifiers. To sum up, NSL-KDD dataset is more reliable to mimic the challenging nature of real-world security issues. [1] and [5] mentioned nothing about the detection precision or accuracy which represent strong indicators of IDS efficiency. All of these aspects causing [1] and [5] less competitive.

In order to further reflect the superiority of our proposed model, Table VI illustrates the accuracy, detection rate, FPR, precision and response time for optimized/hybrid state-of-the-art RBF-based intrusion detection models/systems validated on KDD Cup'99 dataset, in which, the most competitive work to our proposed work in terms of binary classification are Xu *et al.* [7] and Shi *et al.* [8]. However, in terms of class-wise classification, our proposed system is better in terms of both detection rate and FPR. In contrary to state-of-the-art RBF-based schemes, our proposed system shows higher efficiency and reliability, even though it has much lower complexity and it is much easier to implement. That is why high achievable classical RBF-based intrusion detection systems are considered essential blocks in hierarchical on-line adaptive intrusion

detection systems that designed to detect novel and hard-to-detect attacks in hostile real-time environment.

IV. CONCLUSION AND FUTURE WORK

In this work, we formulate the intrusion detection problem in the framework of approximation(interpolation) theory and applying RBFNN as classifier. The accuracy and PPV value of attack classification reached up to 95.78% and 97.11% respectively with high sensitivity to rare attacks (R2L and U2R). However, for this system, we have worked only with 2 phase-RBF training which reflect in relatively low sensitivity towards frequent attacks (DoS and Probe). Therefore, as future work, this system can be enhanced by extending to 3-phase RBF training using different basis functions other than Gaussians and other data representation technique rather than simple k-means algorithm applying on different datasets other than NSL-KDD dataset.

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