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Simple Design Technique for a Triangular FBG Filter Based on a Linearly Chirped Grating

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22 Simple design technique for a triangular FBG filter based on a linearly chirped grating

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30 1. Introduction

17 FBG sensor
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11 ECCLE TO A EXECUTE THE SET ASSEMED AND A SET AND A SET AND A SET AND A SET A A CHE AND A SE 31 ibre Bragg gratings (FBGs) has been widely used in optical com- munications and optical sensing because of their many advantages such as simplicity, low cost, high sensitivity, chemical resistance, multiplexing capabilities and immunity from electrical and mag- netic interference [\[1\].](#page-9-0) In sensing applications, it was widely used in bridge [\[2\]](#page-9-0), petroleum tube and coal mine safety monitoring, river surveillance monitoring, civil structural monitoring, aerospace health monitoring [\[3\]](#page-9-0) etc. For all these applications, it is essential to interrogate the FBG sensor. Due to the high cost of an optical spectrum analyzer (OSA), it is necessary to develop a cost effective method to extract the wavelength information and thus interrogate the FBG sensor. Some FBG interrogation technologies have been 43 developed such as ratiometric approach [4], unbalanced Mach-**Zehnder** interferometers [5] and scanning **Fabry–Perot** filters [6] etc. Among these technologies, ratiometric wavelength measure- ment is a simple, high speed and cost effective scheme compared to wavelength scanning based active schemes [4–8]. In a ratiomet- ric system, the characteristics of the edge filter such as slope and stability will significantly influence the resolution of the system. An FBG has a high stability and a large slope and thus is an ideal de- vice for use as an edge filter and recently has been proposed for interrogation of a FBG sensor [\[9\]](#page-9-0). In [\[10\]](#page-9-0) it was shown that a sin-53 gle–multiple–single mode fibre edge filter used to interrogate a FBG could also be used to compensate temperature induced errors

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ABSTRACT

A novel and simple design technique for triangular spectrum response of fibre Bragg grating (FBG) is pre- 21 sented based on a linear chirped grating. It is shown that this method is fast and can give a straightfor-
22 ward solution to meet a design target. The numerical simulation examples verified the effectiveness of 23 the design method. A general approach to design for multichannel triangular spectral responses for 24 FBG filters is proposed, which provides a solution that achieves a minimum change of refractive index 25 for the fibre. 26

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for the FBG sensor. Since a FBG based edge filter has the same wave-
55 length shift vs. temperature characteristic as a FBG used for sensing, 56 then a FBG edge filter can also compensate for temperature induced 57 errors. Recently Littler [\[11\]](#page-9-0) and Rochette [\[12\]](#page-9-0) have developed an 58 adjustable bandwidth FBG optical filter, which shows that the slope 59 of a FBG edge filter could potentially be adjusted, to allow for an 60 appropriate working wavelength range, by altering the bandwidth 61 of the FBG edge filter. 62

As we know, the FBG normally has a flat top response for the 63 reflective spectrum [\[13\]](#page-9-0) which is not suitable for use as an edge fil-

64 ter. There are several papers concentrating on the design of a trian- 65 gular reflective spectrum response of a FBG by using either a 66 covariance matrix adapted evolution strategy algorithm [\[14\]](#page-9-0) or 67 an accelerated genetic algorithm [\[15\]](#page-9-0). These design methods are 68 based on optimisation methods such as simulated annealing and 69 a genetic algorithm which are complicated and time consuming. 70 An inverse scattering method is a precise and computationally effi-

71 cient method for FBG design [\[16\]](#page-9-0). However, this method still suf- 72 fers from significant complexity. Longhi et al. proposed a simple $\frac{73}{2}$ method using first-order Born approximation [\[17\]](#page-9-0) for FBG spec- 74 trum design. It works in the weak-grating condition (Born approx- 75 imation), which assumes the reflective spectrum shape is 76 proportional to the spatial refractive index modulation profile of 77 the linear chirped FBG. When the refractive index modulation is 78 strong $($ >10⁻⁴), this method fails. Recently Bandyopadhyay et al. 79 reported an empirical design technique of linear edge filter \hat{by} 80 using an apodized linearly chirped fibre grating [\[18\]](#page-9-0). This tech- 81 nique is based on investigating the impact of different apodization 82 functions on the spectrum response of a FBG which will not give a 83

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 straightforward solution to the target. In this paper, a simple and fast design technique for a triangular FBG filter is proposed. By using this technique, a solution will be directly given by a non-lin-87 ear function once a target spectrum is given. This greatly simplifies the design process and saves time and gives a straightforward solu- tion to the desired spectrum. A general approach to design for mul- tichannel triangular spectral responses for FBG filters is proposed, which allows the refractive index modulation to be minimized with a genetic algorithm.

93 2. Theoretical analysis

94 For a fibre Bragg grating, the effective refractive index modula-95 tion can be modeled as [\[19\]](#page-9-0)

$$
\delta n_{\rm eff}(z) = \bar{\delta} n_{\rm eff}(z) \left\{ 1 + v \cos \left[\frac{2\pi}{A(z)} z \right] \right\} \tag{1}
$$

98 Muhere $\bar{\delta}n_{\text{eff}}(z)$ is the "dc" index change spatially averaged over a 99 grating period, χ is the fringe visibility of the index change and nor-100 mally it is 1, $A(z)$ is the grating period and can be expressed as

102
$$
\Lambda(z) = \Lambda_0 (1 + c_p z) \tag{2}
$$

103 where A_0 is the nominal grating period and c_p is the linear chirp 104 coefficient of the grating period. For a uniform grating, $c_{p,\overline{}}=0$ and 105 its maximum reflectivity R_{max} and wavelength are [19]

$$
107 \t R_{\text{max}} = \tanh^2(\kappa L) \t (3)
$$

$$
\lambda_{\text{max}} = \left(1 + \frac{\bar{\delta} n_{\text{eff}}}{n_{\text{eff}}}\right) \lambda_{\text{B}}
$$
(4)

110 γ where L is the grating length, n_{eff} is the fibre effective index, 111 $\lambda_{\rm B} = 2n_{\rm eff}$ is the designed Bragg wavelength, κ is "AC" coupling 112 coefficient which can be expressed as [19]

$$
114 \qquad \kappa = \frac{\pi}{\lambda} \bar{\delta} n_{\text{eff}} \tag{5}
$$

115 A chirped grating of length L can be divided into N uniform grat-116 ings of length L_s as illustrated in Fig. 1.

Fig. 1. Structure of chirped fibre Bragg grating.

The chirped grating consists of N uniform gratings. Each section 117 has its own "dc" index change $\bar{\delta}n_{\text{eff}}(z)$ and grating period Λ_i . All the 118 sections have the same length L_s and $\frac{1}{9}$

$$
A_i = A_0 + c_p(z_i - L/2) \qquad 0 \leqslant z_i \leqslant L \tag{6}
$$

Our design principle is to treat each section as a separate uni- 122 form grating with an individual centre wavelength and maximum 123 reflectivity. In order to get a triangular spectrum response, we as- 124 sume the maximum reflectivity of each section is a triangular func-
125 tion of wavelength, which can be defined either using a log scale 126 127

$$
\begin{cases}\n10\lg\{\tanh^2[\kappa(z)L_s]\} = a\lambda + b & \lambda_0 \le \lambda \le \lambda_1 \\
10\lg(\tanh^2[\kappa(z)L_s]) - a\lambda + d & \lambda \le \lambda \le \lambda\n\end{cases}
$$
\n(7a)

$$
\left(10\lg\{\tanh^2[\kappa(z)L_s]\}=c\lambda+d\quad \lambda_1\leqslant \lambda\leqslant \lambda_2\right)\qquad \qquad 129
$$

$$
\mathbf{Qr} \text{ using a linear scale:} \tag{130}
$$

 $\boldsymbol{\kappa}$

$$
\begin{cases}\n\tanh^2[\kappa(z)L_s] = a\lambda + b & \lambda_0 \le \lambda \le \lambda_1 \\
\tanh^2[\kappa(z)L_s] = c\lambda + d & \lambda_1 \le \lambda \le \lambda_2\n\end{cases}
$$
\n(7b)

where a, b, c and d are constants, and μ and μ and μ and μ and μ and μ are μ are μ are μ and μ are μ are μ

$$
\lambda_0 = 2n_{\text{eff}}(A_0 - c_p L/2) \n\lambda_1 = 2n_{\text{eff}}(A_0 + c_p z_1 - c_p L/2)
$$
\n(8)

$$
\lambda_2 = 2n_{\text{eff}}(A_0 + c_p L/2) \tag{136}
$$

$$
E(z) = \frac{\pi}{\lambda_{\text{max}}} \bar{\delta} n_{\text{eff}}(z)
$$

$$
=\frac{n}{2[n_{\text{eff}}+\bar{\delta}n_{\text{eff}}(z)](A_0+c_pz-c_pL/2)}\bar{\delta}n_{\text{eff}}(z).
$$
\n(9)

Once we set our desired triangle, the parameters q , b , c and d are gi- 140 ven, then the refractive index change $\bar{\delta}n_{\text{eff}}(z)$ can be directly given 141 by Eq. (7). By using the parameters of $\bar{\delta}n_{\text{eff}}(z)$ from (7), we can 142 achieve a designed triangular spectrum response for the FBG. 433

3. Numerical stimulations 144

To demonstrate the effectiveness of the triangular spectrum de- 145 sign method above, numerical simulations on FBG were provided. 146 The simulations were based on well-known transfer matrix meth- 147 od which was developed by Yamada et al. [\[20\]](#page-9-0). . 148

As a first pass, we assumed the target spectrum has a log scale 149 with values $z_1 = L/2$, $\lambda_0 = 1550$ nm, $m = a\lambda_0 + b = c\lambda_2 + d = -25$, 150 $n = a\lambda_1 + b = c\lambda_1 + d = -5$, $c_{p} = 1.57$ nm/cm, and $L_s = 100$ μ m, 151 $L = 30$ mm. By solving Eq. (7a) we can get the refractive index mod- 152 ulation coefficient distribution $\bar{\delta}n_{\rm eff}(z)$ along the grating length as 153 shown in Fig. 2a. However, it was found that the value of $\bar{\delta}n_{\text{eff}}(z)$ Þ 154 we get from $(7a)$ is so large that the reflectivity of the grating is 155

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156 close to 100% resulting in a flat reflective spectrum response of the 157 FBG which is shown in [Fig. 2b](#page-3-0).

 To overcome this problem it is necessary to reduce the value of 159 the refractive index modulation coefficient $\bar{\delta}n_{\text{eff}}(z)$ and keep its shape unchanged. Hence a scaling factor W is applied to the calcu-161 lated refractive index modulation coefficient $\bar{\delta}n_{\text{eff}}(z)/W$ to get a de- sired triangular spectrum response. Fig. 3 shows the simulation results for the influence of scaling factor W on the spectral re-sponse of the FBG.

Fig. 3 shows that with a reduced index modulation, a triangular 165 reflective response for the FBG can be achieved when the peak 166 reflectivity of the FBG is less than 90% (corresponding to $W > 5$ in 167 this case). As the scaling factor increases, the peak reflectivity de- 168 creases but the shape of the triangular spectral response remains 169 unchanged. 170

In selecting a value for *, one approach is to assume a reason- 171* able value of reflectivity, such as 50%, a value of *= 10 is therefore 172* chosen for use in further simulations. Using a constant value of 173

Fig. 3. Calculated (a) index modulation and (b) spectral response of the FBG by introducing a constant factor W = 5, 7, 10, 15 and 20.

Fig. 4. Calculated (a) index modulation and (b) spectral response of the FBG with different shape.

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174 $W = 10$ for the index modulation, an investigation on the effect of 175 $\,$ changes to m and n on the spectral response were carried out 176 and are shown in [Fig. 4](#page-4-0) .

177 By setting different values of m and μ , a triangular reflective re-178 sponse of FBG with different discrimination can be achieved simply 179 by using the corresponding refractive index modulation shown in 180 Fig. $4a$. However, Fig. $4b$ also shows that the fluctuation of the 181 reflectivity in the edge filter wavelength range is excessive espe-182 cially for the FBG with $m = -15$ and $n = -5$. This is due to the 183 non-apodized refractive index modulation at both sides of the grat-184 ing. In order to eliminate the reflectivity fluctuation, an apodized refractive index modulation with a sin function is applied to both 185 sides of the grating for a 2 mm length. [Fig. 5](#page-4-0) gives the simulated 186 results for both non-apodized and apodized refractive index mod- 187 ulated FBG. 188

[Fig. 5](#page-4-0)_b shows that with an apodized index modulation as shown 189 in Fig. $5a$, the reflective spectrum of the FBG becomes much 190 smoother. This indicates that apodization of the index modulation 191 on both sides will reduce the fluctuation of the reflective spectrum 192 of the designed FBG. All the simulations below are based on a sin 193 function apodization for a 2 mm length for both sides of the 194 grating. 195

Fig. 6. Calculated index modulation and reflective spectral response of the FBG with (a) $z_i = L/3$ and (b) $z_i = L/1.5$.

Fig. 7. Calculated (a) index modulation and (b) reflective spectral response of the FBG with c_p = 3.14, 1.57 and 0.31 nm/cm, respectively.

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196 If we want to design an asymmetrical triangular spectrum, the 197 only thing we need to do is to reset z_1 to a desired value and keep-198 ing other parameters unchanged. [Fig. 6](#page-5-0) gives simulation results for 199 z_{1⁄}= L/3, 2L/3, respectively.

200 [Fig. 6](#page-5-0) shows that by using the refractive index modulation 201 provided, an asymmetrical triangular spectrum can be easily 202 obtained.

203 To investigate the influence of linear grating period's chirp coef-204 ficient c_p on the reflective spectrum of the FBG, simulations were carried out by setting different c_p . [Fig. 7](#page-5-0) gives the simulation re- 205 sults for $c_{p,\overline{z}}$ 3.14, 1.57 and 0.31 μ m/cm, respectively. $\hspace{1.5cm}$ 206

[Fig. 7](#page-5-0) shows that with different c_p , in order to have similar peak \qquad 207 reflectivity, the FBG should have different refractive index modula- 208 tion (and hence different scaling factor $\cancel{\mathsf{W}}$). The larger the c_{p} , the 209 smaller the scaling factor W. In all cases, the designed gratings 210 have triangular spectrum as shown in [Fig. 7](#page-5-0)<u>b</u>. Fig. 7<u>b</u> also shows 211 that the peak wavelength is slightly different for different $c_{\rm p}$. This \quad 212 is because comparing to a lower refractive index modulation, a 213

Fig. 8. Calculated (a) index modulation and (b) reflective spectrum response of the FBG with grating length L = 10, 20, 30, 40 and 50 mm, respectively.

Fig. 9. Calculated (a) index modulation and (b) spectral response of the FBG with different reflectivity but a symmetrical triangular spectrum and (c) index modulation and (d) spectral response with an asymmetrical triangular spectrum.

226

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214 higher index modulation will result in a longer Bragg wavelength 215 as described in Eq. [\(9\)](#page-3-0) .

216 The influence of grating length L on the triangular spectrum re-217 sponse of designed FBG was also studied and the simulation results 218 were shown in [Fig. 8](#page-6-0) .

 From [Fig. 8](#page-6-0) one can see that as grating length increases, the reflective spectrum response of the FBG becomes smoother at the triangular response area. This indicates that the design method in this paper is more suitable for a longer grating length.

 Simulations for the target spectrum with a linear scale have been also carried out and the simulation results are shown in [Fig. 9](#page-6-0). In our simulation, the parameters used are: $z_{1,\overline{\zeta}}$ L/2, λ_{0} = 1550 nm, $m = a\lambda_{0x} + b = c\lambda_{2x} + d$, $n = a\lambda_1 + b = c\lambda_1 + d$, c_{p} = 1.57 nm/cm, and L_{s} = 100 µm, $L = 30$ mm, $W = 14$. By solving $\frac{Eq.}{10}$ (7b) we can get the refractive index modulation coefficient dis-**in the follocal incide of the grating length.** In order to eliminate fluctuations in the reflectivity, an apodized refractive index modu- lation using a sin function is also applied to both sides of the grat-ing for a 2 mm length.

233 [Fig. 9](#page-6-0) shows that with above design method, a triangular spec-234 tral response, using a linear scale, can be easily achieved.

235 The limitation in terms of the bandwidth is also investigated. To 236 study this, a reflective bandwidth of 1 nm for a triangular spectrum 237 was investigated but with two different sets of parameters: one 238 grating has a long length (120 mm) but with a small chirp coeffi-239 cient (0.031 nm/cm) ; the other grating has a short length 240 (30 mm) but with a relatively large chirp coefficient (0.142 nm) 241 $\frac{cm}{cm}$. Both gratings have a similar peak reflectivity of 90% and band-242 width of 1 nm . The simulation results are shown in Fig. 10.

Fig. 10₂ shows that the shorter grating needs a higher refractive 243 index modulation compared to longer grating in order to have a 244 similar peak reflectivity. Fig. 10₂ shows that the longer length grat- 245 ing has smooth spectral response. This indicates that our method 246 could be used to design a triangular spectrum with a bandwidth 247 as low as 1 nm . Our further investigations show that even when 248 the bandwidth is as low as 0.5 nm, the reflective spectral response 249 is still smooth. However, as shown in Fig. $10b$, the spectral re- 250 sponse is not smooth when the grating length is less 30 mm . This 251 is a result of the trade-off between the filter bandwidth and grating 252 length. 253

4. Tolerance of the design method to fabrication errors 254

The fabrication of a triangular FBG requires complex refractive 255 index control and minor errors in fabrication will inevitably occur. 256 We investigated the effect of a perturbation of the amplitude of the 257 refractive index modulation on the designed FBG. To do this a per- 258 turbation factor $\alpha(z)$ is added to $\bar{\delta}n_{\text{eff}}(z)$ which can be expressed as 259 follows: 260

 $\delta' n_{\text{eff}}(z) = \delta n_{\text{eff}}(z)[1 + \alpha(z)]$ (10) 262

where $\bar{\delta}n_{\rm eff}(z)$ is the required value obtained from [Eq. \(7\).](#page-3-0) The typ- 263 ical distribution of fabrication errors follows a normal distribution. 264 Thus we assume $\alpha(z)$ has a normal distribution with a mean 0 and 265 standard deviation 1 (e.g. $|x| < 5\%$ means that the value of α is gen- 266 erated randomly with a normal distribution with a mean 0 and 267 deviation 1 in the range \pm 5%). 268

Fig. 10. Calculated (a) index modulation and (b) spectral response of the FBG with different grating length and chirp coefficient.

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Fig. 12. Designed four-channel triangular FBG spectrum (a) amplitude profile (b) fine detail of the amplitude profile (c) phase profile (d) expanded section of the phase profile and (e) reflective spectrum.

269 Based on the method above, simulations were carried out using 270 as an example the parameters for the longer grating in Fig. 10. The 271 simulation results are shown in Fig. 11 .

[Fig. 11](#page-7-0)b shows a comparison of the reflective spectra when 273 $|\alpha|$ = 0, <5% or <10%. It can be seen that the corresponding variation of the reflectivity is small although the variations of the refractive index modulation are significant as shown in [Fig. 11](#page-7-0)a. This indi- cates that when the refractive index modulation perturbation is 277 in the range of $|\alpha| < 10\%$, the fabricated spectral response of a trian-gular FBG is still acceptable.

279 5. Multichannel triangular spectra design

280 It is also possible to use the design approach above to achieve 281 multichannel triangular spectra by using the general multichannel 282 design method in [\[21,22\]](#page-9-0). The general expression of M-channel

FBG takes a form of a superposition of M individual constituent 283 gratings: 284

$$
^{285}
$$

) 295

$$
Q(z) \exp\{i[K_0 z + \varphi(z)]\} = \sum_{m=1}^{M} \bar{\delta}_m(z) \exp[i(K_0 z - K_0 \Delta \lambda_m z / \lambda_0 - K_0 c_p z^2 + \phi_m)]
$$
(11) 287

where $Q(z)$ is the amplitude function of the composite grating and \qquad 288 K_0 is its propagation constant and is related to the fundamental 289 grating period A_0 by $K_0 = 2\pi/A_0$. $\varphi(z)$ is the phase factor of the comgrating period A_0 by $K_0 = 2\pi / A_0$. $\varphi(z)$ is the phase factor of the com- 290 posite grating. $\bar{\delta}n_{\text{eff}}(z)$ and ϕ_m are the refractive index modulation 291 and phase functions of the mth constituent grating. $\Delta\lambda_m$ is the chan-
292 nel spacing of the mth grating from the fundamental grating wave-
293 length λ_0 . 294

The complex Eq. (11) can be solved for the phase function $\phi(z)$ and the amplitude function $Q(z)$ to obtain \sim 296

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$$
\varphi(z) = \tan^{-1} \left[\frac{\sum_{m=1}^{M} \bar{\delta}_m(z) \sin[K_0 z - K_0 \Delta \lambda_m z / \lambda_0 - K_0 c_p z^2 + \phi_m]}{\sum_{m=1}^{M} \bar{\delta}_m(z) \cos[K_0 z - K_0 \Delta \lambda_m z / \lambda_0 - K_0 c_p z^2 + \phi_m]} \right]
$$

$$
Q(z) = \sqrt{\left(\sum_{m=1}^{M} \bar{\delta}_m(z) \cos[K_0 z - K_0 \Delta \lambda_m z / \lambda_0 - K_0 c_p z^2 + \phi_m]\right)^2 + \left(\sum_{m=1}^{M} \bar{\delta}_m(z) \sin[K_0 z - K_0 \Delta \lambda_m z / \lambda_0 - K_0 c_p z^2 + \phi_m]\right)^2}
$$

297 Eqs. (12) and (13) are the design equations for multichannel tri-298 angular FBG filters. The amplitude refractive index modulation for 299 a single FBG can be obtained from [Eq. \(7\)](#page-3-0) and the complex phase 300 and amplitude modulation can be solved from Eqs. (12) and (13). 301 The amplitude function $\mathcal{Q}(z)$ can be minimized by systematically 302 $\;$ obtaining an optimal set of the phase ϕ_m of the constituent gratings 303 as proposed by Kolossovski [23] .

304 As an example, we simulated a four-channel triangular FBG 305 filter. In our simulations, the parameters used are: $M = 4$, λ_{0} = 1550 nm, n_{eff} = 1.485, z_{1} = L/2, c_{p} = 0.4 nm/cm, $m = -35$, n = $-5, \, \not k = 30 \text{ mm}$ and $\Delta \lambda = 4 \text{ nm}$,

308 As a result, the optimal set of ϕ_m is {2.074, 3.808, 1.117, 5.984} 309 and the maximum amplitude modulation is 4.17×10^{-4} , which is 310 only twice that of the single triangular FBG, that is $\frac{2.09}{2} \times 10^{-4}$. 311 The calculated results were shown in Fig. $12a$ –e.

 Fig. $12a-d$ shows the amplitude and phase modulation of the 313 – multichannel triangular FBG and Fig. 12g shows the reflective spectrum of the designed FBG. It can be seen that by using both amplitude and phase modulation with a grating length of only 30 mm, we can obtain four channels with a triangular spectral response.

318 6. Conclusion

306

307

re the desire quadratic first material three contents and the convention of multiple effective index modulation for

a amplitude refractive index modulation for
 Q_2^2 (and the complex phase (1) and (2)

116. Research w In this paper, we have presented a new and simple design method for a triangular spectral response for an FBG based on a lin- ear chirped grating. This method can give a straightforward solu- tion to the design target by only solving a non-linear function. Compared to the existed methods [14–16], this method is simple and fast. Moreover a multichannel design for a triangular spectrum is also provided based on our previous optimum design method – and refractive index modulation can be minimized by using genet- ic algorithm. The numerical simulation examples verified that the proposed design method is effective.

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