Misalignment Limits for a Singlemode-multimode-singlemode Fiber-based Edge Filter

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Abstract—Misalignment effects on the spectral characteristics of edge filters based on singlemode–multimode–singlemode (SMS) fibre structures are investigated numerically and experimentally. A modal propagation analysis is used with a set of guided modes calculated using the finite-difference method to determine the transmission loss of the SMS-based edge filters. A limit for the tolerable misalignment of the SMS fiber-based edge filter is proposed, beyond which the spectral performance of the SMS structure degrades unacceptably. The numerical results are verified experimentally with good agreement.

Index Terms—Edge filter, multimode interference, optical fibers.

I. INTRODUCTION

SINGLEMODE–MULTIMODE–SINGLEMODE (SMS) fiber structures have been investigated for use in several applications, e.g., as a refractometer, a bandpass filter, and an edge filter [1]–[4]. An optical device based on the SMS fiber structure offers an all-fiber solution for optical communications and optical sensing applications with the advantages of simplicity of packaging and ease of interconnection to other optical fibers.

The SMS structure is fabricated by splicing a precisely dimensioned multimode fiber (MMF) section between two single-mode fibers (SMFs). Ideally, the center axes of all the fibre cores are precisely aligned. However, in practice the splicing process itself, along with the manufacturing variations in core-cladding concentricity can introduce lateral misalignment between the centers of the SMF–MMF–SMF cores.

In [2], [4], and [5], the SMS fiber structure is analyzed using a modal propagation analysis (MPA) for the linearly polarized (LP) (or scalar) modes. The input light can be assumed to have the field distribution of the fundamental mode of the SMF [5]. When the light launches into the MMF, the input field can be decomposed into the eigenmodes (LPmn) of the MMF. Due to the circular symmetric nature of the input field and an ideal alignment assumption, the number of guided modes of the MMF used in the modal propagation analysis is greatly reduced from LPmn to LP0m or the circular symmetry modes. This reduced number of modes means the calculation can be performed efficiently. In [1] and [3], the SMS structure is investigated using the beam propagation method, where it is assumed that only the circular symmetry modes exist. With this assumption the optical field is simplified so that it is independent of the angular coordinate in a cylindrical coordinate system. However, if the center (or meridional) axes of the SMS cores are misaligned relative to one another then we cannot assume circularly symmetrical modes. Thus, both approaches published so far cannot be used to study the effect of misalignment in an SMS structure.

An MPA using a complete set of hybrid modes or vectorial form guided modes in the MMF has been proposed to analyze the misalignment effect [6]. In this approach, a complete set of guided modes in the MMF is calculated and an adaptive algorithm is developed to perform mode expansion of the optical field in the MMF. However, the complete set of guided modes in the MMF can also be solved with an alternative numerical method, the finite difference method (FDM) [7]. The numerical approach using FDM offers simplicity of its implementation. In this paper, the FDM is used to calculate the complete set of guided modes in the MMF and then the MPA is performed to analyze the misalignment effect. Building on previous research on an SMS-based edge filter [3], [4], in this paper, the effect of fiber misalignment within an SMS-based edge filter is investigated both numerically and experimentally, so as to establish an upper limit on tolerable misalignment above which the performance of SMS structure is degraded significantly.

To put the misalignment induced performance degradation in context, the application chosen here for the SMS is that of an edge filter used within a ratiometric wavelength measurement system. A ratiometric wavelength measurement usually consists of a 3-dB coupler which the two outputs connect to an edge filter arm with a well-defined spectral response and a reference arm, or alternatively two edge filter arms with opposite slope spectral responses can be used. The use of two opposite slope edge filters can increase the usable resolution of the ratiometric system [8]. A ratiometric wavelength measurement based system on two opposite slope SMS-based edge filters is built and demonstrated in this paper.

II. SMS-BASED EDGE FILTERS

A schematic structure for a ratiometric wavelength measurement consisting of two SMS-based edge filters is shown in Fig. 1(a). The target spectral responses in dB of the SMS-based edge filters are shown in Fig. 1(b), and can have either a negative (P1) or a positive (P2) slope. Two key parameters for an edge filter are baseline loss and discrimination range. The
SMS-based edge filter operates over a wavelength range from \( \lambda_1 \) to \( \lambda_2 \) with a progressively larger or smaller transmission loss as the wavelength increases from \( \lambda_1 \) to \( \lambda_2 \), for the negative or positive slope, respectively. The baseline loss is defined as the transmission loss of the filter at \( \lambda_1 \) or \( \lambda_2 \), for the negative and the positive slopes, respectively, while the discrimination range is the difference between the transmission loss at \( \lambda_1 \) and \( \lambda_2 \). The corresponding ratio (P2–P1) of the two outputs over the wavelength range is presented in Fig. 1(c). The wavelength of an input signal can be determined through measuring the power ratio of the output ports at the outputs of the two arms, assuming that a suitable calibration has taken place.

The fiber structure under consideration consists of an input SMF, a sandwiched MMF section, and an output SMF, as shown in Fig. 2(a). The concentric alignment and misalignment conditions in the Cartesian coordinate system, between the input SMF, MMF section, and output SMF cores, are shown in Fig. 2(b) and (c), respectively. The radii of SMF and MMF are denoted as \( R_s \) and \( R_m \), respectively. The input SMF and output SMF positions are denoted by the coordinates \( I[x, y] \) and \( O[x, y] \), respectively, where \( x \) and \( y \) are in \( \mu m \).

### III. Modal Propagation Analysis

The MMF section can support many guided modes and the input field is reproduced as single image at periodic intervals along the propagation direction due to the interference between these guided modes. This is the so-called self-imaging principle and the distance at which self-imaging occurs is called the re-imaging distance. The approach used here to analyze the field distribution in the MMF section is a modal propagation analysis [9]. In the MMF, an MPA using a cylindrical coordinate system has been employed in [2], [4], and [5] based on a scalar approximation of the LP_{0n} modes. The LP_{0n} modes could not be used to investigate misalignment effects because it only consists of circularly symmetrical modes. To analyze misalignment it is necessary to calculate a complete set of guided modes in the MMF [6]. In the approach used here, the MPA is performed in the Cartesian coordinate system with a set of calculated guided modes using FDM to allow investigation of misalignment effects.

The MPA procedure is as follows: the input light is assumed to have the field distribution \( \psi(x, y, 0) \) of the fundamental mode of the SMF. The input field can be decomposed into the eigen-modes of the MMF, \( \phi_{\nu}(x, y) \), when the light enters the MMF section. The input field at the MMF can be written as

\[
\psi(x, y, 0) = \sum_{\nu} c_{\nu} \phi_{\nu}(x, y)
\]
where $c_{\nu}$ is the excitation coefficient of each mode. The coefficient $c_{\nu}$ can be calculated by an overlap integral between $\psi(x,y,0)$ and $\varphi_{\nu}(x,y)$

$$c_{\nu} = \frac{\int \psi(x,y,0)\varphi_{\nu}(x,y)dxdy}{\sqrt{\int \varphi_{\nu}^2(x,y)dxdy}} \tag{2}$$

As the light propagates in the MMF section, the field at a propagation distance $z$ can be calculated by

$$\psi(x,y,z) = \sum_{\nu} c_{\nu}\varphi_{\nu}(x,y)\exp[j\beta_{\nu}z] \tag{3}$$

where $\beta_{\nu}$ is the propagation constant of each eigenmode of the MMF. The transmission loss in dB can be determined by using the overlap integral method between $\psi(x,y,z)$ and the eigenmode of the output SMF $\psi_0(x,y)$

$$L_s(z) = 10\log_{10}\left(\frac{|\int \psi(x,y,z)\psi_0(x,y)dxdy|^2}{\int |\psi(x,y,z)|^2 dxdy \int |\psi_0(x,y)|^2 dxdy}\right) \tag{4}$$

Here $\varphi_{\nu}(x,y)$ and $\beta_{\nu}$ can be obtained by using a semivectorial FDM. It should be noted that FDM calculates a set of all possible guided modes in the MMF section, not just concentric circular modes, allowing the transmission loss due to misalignment to be calculated. Using the above equations, the light propagation in the whole structure can be analyzed.

IV. DESIGN EXAMPLE AND SPECTRAL RESPONSE

To investigate the effect of misalignment, in the first instance it is necessary to present a typical SMS structure designed to meet a target spectral response and calculate its ideal, perfectly aligned, spectral response.

To design the SMS-based edge filter, the MMF length needs to be determined. It has been shown that the re-imaging distance is wavelength dependent [2], [5]. If re-coupling into the output SMF takes place at the re-imaging distance, then the MMF section of the SMS structure has by definition a length equal to the re-coupling distance and operates as a bandpass filter as in [2] and [5]. However, for the purpose of designing an edge filter, the bandpass response can be considered as two spectral responses, on either side of a center wavelength. Consequently, the device can behave as an edge filter for a selected wavelength range. Two SMS-based edge filters with opposite slope spectral responses within a given wavelength range can be obtained by choosing two bandpass filters with appropriate center wavelengths [4].

As an example to illustrate the design process, a target wavelength range for wavelength measurement from $\lambda_1 = 1520$ nm to $\lambda_2 = 1545$ nm is chosen. This range is chosen as it corresponds to the typical center wavelengths for many fiber Bragg grating (FBG) sensors. Based on the target spectral responses as in Fig. 1(b), the SMS-based edge filters are designed with the baseline loss $>8$ dB and the desired discrimination range $>8$ dB. A standard SMF28 fiber is chosen as the SMF, for which the parameters are: the refractive indices for the core and cladding are 1.4504 and 1.4447, respectively (at a wavelength of 1550 nm), and the radius of the core $R_s = 4.15 \mu m$. An MMF-type AFS105/125Y is chosen as the MMF section for which the parameters are: refractive indices for the core and cladding are 1.4446 and 1.4271, respectively, with a core radius $R_m = 52.5 \mu m$. The small difference between the refractive indices of the SMF and MMF means that the Fresnel reflection occurring at their interface is negligible (the level of reflection is $-54$ dB or lower relative to the injected light level) and a one-way modal propagation analysis can be used [5]. As mentioned above, for the specified wavelength range, two opposite response slope edge filters (negative and positive slopes) can be obtained by designing two bandpass filters with peak wavelengths: $\leq 1520$ nm and $\geq 1545$ nm, respectively. From (10) in [5], the peak wavelengths from 1500 to 1520 nm correspond to the MMF lengths $L = 44.25$–43.66 mm, and from 1545 to 1560 nm correspond to $L = 43.00$–42.58 mm. Suitable peak wavelengths for the targeted wavelength range are 1510 and 1547 nm and the corresponding MMF lengths are $L = 43.96$ mm and $L = 42.95$ mm, for the negative and positive slope edge filters, respectively. The peak wavelengths at 1510 and 1547 nm are chosen for the SMS-based edge filters because their transmission loss responses have a suitable spectral response over the targeted wavelength range from 1520 to 1545 nm. The calculated transmission loss responses by using (4) for the designed SMS-based edge filter are shown in Fig. 3. These responses represent the performance of the design example for the case of perfect alignment. It can be seen that the two opposite edge filter responses within the targeted wavelength range can be achieved using two bandpass filters. The calculated negative and positive slope responses of the SMS-based edge filters from 1520 to 1545 nm have a transmission loss from $-7.20$ to $-15.53$ dB and $-11.84$ to $-0.77$ dB, respectively, and the corresponding discrimination ranges are $8.33$ dB and $11.06$ dB, respectively, suitable for use as edge filters.
To investigate the misalignment effect, the transmission loss of several positions of the input SMF and output SMF are calculated using (4). We calculated the transmission loss within the wavelength range 1520–1545 nm of the offset positions, $f(a, 0)$, $O(0, a)$, where $a = 0$–$10 \mu m$ with an increment of $2 \mu m$. Given the need to undertake experimental verification, these misalignment values are chosen based on the deliberate offset that can be produced by the fusion splicer used in the experiments described later. The calculated transmission loss responses are shown in Fig. 4(a) and (b), for the negative and positive slope edge filters, respectively. From Fig. 4(a), for the negative slope, it can be seen that, even with misalignment, the response retains a monotonically decreasing characteristic over the wavelength range and thus is still suitable for use as the edge filter response. However, the discrimination range decreases as the offset increases, from 8.33 dB without an offset to 8.03, 7.41, 6.64, 5.93, and 5.15 dB for an offset equal to 2, 4, 6, 8, and $10 \mu m$, respectively. A reduced discrimination range will have a negative impact on measurement accuracy where the edge filter is used within a ratiometric wavelength measurement system. For the positive slope filter, as shown in Fig. 4(b), the response slope changes very significantly when the offset increases. For an offset $a = 2$ and $4 \mu m$ the spectral responses are still suitable as the edge filter, but for larger offset values the transmission loss responses do not monotonically increase across the wavelength range and therefore are not suitable for use as an edge filter.

The change in the negative and positive slopes due to an offset needs to be considered in the context of changes to the overall bandpass responses. The consequences of an increase in the offset on the bandpass response are a shift of the self-imaging position and a reduction in the maximum transmission loss at the peak wavelength of the bandpass filter. Such changes in the overall bandpass response will also clearly change the positive and negative slope responses.

In practice, there is a significant difference between the negative and positive slope responses in terms of the change in the response that is induced by an offset. This difference can be explained as follows. From the MPA discussed above and as described in [6], the presence of an offset for the input SMF increases the number of excitation modes (circularly symmetrical modes and azimuthal modes) compared to the case without an offset (circularly symmetrical modes only). Increasing the number of excitation modes changes the MMF field pattern resulting from interference in the MMF. In turn, the transmission loss, which is a function of the overlap between the MMF field and the eigenmode of the output SMF, varies with changes in the offset of the output SMF.

To better understand the difference in the manner in which an offset affects the negative and positive slopes, the MMF field amplitude profiles for the cases of $a = 0 \mu m$ and $a = 10 \mu m$ are shown in Fig. 5 for a wavelength of 1537 nm. This wavelength is chosen as it corresponds to the wavelength at which the changes in the positive slope are most pronounced, as shown in Fig. 4. The MMF field amplitude profiles for the negative slope response for the case of $a = 0 \mu m$ and $a = 10 \mu m$ are shown in Fig. 5(a) and (b), respectively. The overlap between the MMF field amplitude profile and the eigenmode of the output SMF is located at $O[0, 0]$ and $O[0, 10]$ in $\mu m$, for the case of $a = 0 \mu m$ and $a = 10 \mu m$, respectively. Comparing Fig. 5(a) and (b), there is only a relatively small difference in the amplitude of the MMF field in the MMF overlap region when an offset is introduced. As a result, the transmission losses are not strongly influenced by offset.

For the positive slope response, the MMF field amplitude profile for the case of $a = 0 \mu m$ and $a = 10 \mu m$ is shown in Fig. 5(c) and (d), respectively. Comparing these figures, it can be seen that when an offset is introduced, that is $a = 10 \mu m$, the eigenmode of the output SMF located at $O[0, 10]$ overlaps a portion of the MMF field amplitude profile which has a very low value. The result is a very high transmission loss when an offset is introduced and thus there is a strong dependence of the transmission loss on offset.

To further analyze the spectral quality of the edge filter, it is necessary to examine the linearity of the transmission loss when misalignment occurs. Linearity is important for an edge filter used in wavelength measurement application for two reasons.
First, a linear response by definition monotonically increases or decreases, so there can be no ambiguity in wavelength measurements. Second, a linear response will ensure that the resolution for wavelength measurement is the same for all measured wavelengths. The linearity can be examined by using the correlation coefficient \( R^2 \) of the linear regression analysis. An ideal spectral response has \( R^2 = 1 \), and a lower \( R^2 < 1 \) indicates a lower quality for the spectral response linearity. Fig. 6 shows the correlation coefficient for the different offsets from 0 to 10 μm with an increment of 1 μm. It is shown that for the negative slope, the \( R^2 \) maintains a high value and is almost constant with \( R^2 = 0.98, 0.98, 0.99, 0.99, 0.99, 0.99, \) and 0.99 for the offset \( \alpha = 0, 2, 4, 6, 8, \) and 10 μm, respectively. This means that the offset has little effect on the slope quality for the negative slope spectral response, but does reduce the discrimination range as mentioned above. For the positive slope, it is clear that the offset affects the slope quality. The \( R^2 \) are 0.98, 0.99, 0.99, 0.67, 0.28, and 0.07 for the offset of 0, 2, 4, 6, 8, and 10 μm, respectively. The \( R^2 \) value degrades beyond an offset value of \( \alpha = 5 \) μm, with \( R^2 = 0.95 \), and such spectral responses are not suitable for use in an edge filter. Based on the calculation of the \( R^2 \) value, it is suggested as a conservative guiding principle that the misalignment should be less than the core radius of the SMF (4.15 μm in this case) to maintain the slope quality for the two SMS-based edge filters with opposite spectral responses.

For the purpose of experimental verification, the two SMS-based edge filters were fabricated using a precision Fujikura CT-07 cleaver and a Sumitomo type-36 three-axis fusion splicer. For each SMS structure the process is the same. First, the input SMF and the input end of the MMF are cleaved and spliced together. To deliberately introduce an offset (and thus misalignment) in this splice, an attenuation splicing mode, available as an option on the fusion splicer, is used. This splicing mode allows for the creation of a fiber splice with a preset optical power loss. Given a preset power loss, the fusion splicer will automatically perform the splice with an appropriate axial offset.

The cleaver is again used to precisely cleave the un-terminated end of the MMF fiber so that its length is set to the desired value. Finally, the output end of MMF section is spliced to the cleaved end of the output SMF, again with the attenuation splicing option. The desired power loss is set so that it corresponds to an offset of 3.3 μm.

The transmission loss response of each fabricated filter is measured using a tunable laser and an optical spectrum analyzer (OSA). The measured results are shown in Fig. 7 for the
negative and the positive slope SMS-based edge filters. The calculation of transmission loss using (4) is also shown in Fig. 7. The calculated and measured results show a good agreement. The discrepancy between the calculated and measured results is most likely a result of: 1) residual splicing insertion losses and 2) errors in the exact length of the MMF section. MMF section length errors, which arise during fabrication of the SMS structure, shift the peak wavelength of the bandpass filter response, which in turn alters the measured transmission loss values over a fixed wavelength range.

Experimentally the two edge filters with their deliberate misalignment, while they do possess a higher insertion loss, demonstrate response slopes with an acceptable discrimination ranges of 9.47 and 8.89 dB for the negative and positive slopes, respectively. The edge filters are therefore still suitable for use as edge filters. This result verifies our assertion that as long as the misalignment between SMF and MMF cores is less than an offset misalignment limit which is equal to the SMF core radius then there is no significant effect on the slope quality.

To provide confirmation a misaligned SMS-based edge filter will work as long as the lateral misalignment in an SMS structure is less than the limit proposed, the edge filter described above with a 3.3 μm lateral misalignment was employed in a functioning wavelength measurement system, based on the scheme described in Fig. 1(a). The input signal is split into two equal intensity signals using a 3 dB fiber splitter. One of the signals passes through the negative slope SMS-based edge filter and the other passes through the positive slope SMS-based edge filter. A dual channel power meter is placed at the ends of both arms. Fig. 8 shows the measured ratio of the optical power. The measured ratio between 1520 and 1545 nm has a linear slope with a discrimination range of 18.14 dB from 7.17 to 10.97 dB, which is suitable for wavelength measurement.

It should be noted that for the fabrication of an SMS, it is preferable to use a fusion splicing machine with the capability of three-axis adjustment rather than a single-axis (also called a fixed V-groove) fusion splicer. Lateral misalignment arises in an SMS structure for two reasons. First, there is the lateral misalignment introduced by the fusion splicer itself, and second, there is the misalignment that results from the limited manufacturing tolerance of core-cladding concentricity of the fibers used. Using a fusion splicer with three-axis adjustment can negate the effect of the limited core-cladding concentricity of the fibers. This means that the only significant source of misalignment is the inherent alignment accuracy of the fusion splicer itself. Typical three-axis adjustment splicers can maintain inherent misalignment to less than 0.5 μm in the case of identical SMF or MMF splicing and thus can allow the fabrication of SMS structures with repeatably low lateral misalignment. The use of a single-axis fusion splicer is less advisable for SMS fabrication as it is not possible to overcome misalignment due to limited core concentricity and furthermore a single-axis splicer typically has an inherent misalignment that is higher than a three-axis adjustment splice machine.

VI. CONCLUSION

The effect of misalignment on the spectral response of an SMS-based edge filter has been investigated. An MPA with a
calculated set of guided modes using FDM is employed to analyze the misalignment effect. It is shown that the performance of the SMS based edge filter degrades when the lateral misalignment is larger than a misalignment limit which is equal to the core radius of the SMF used. The measured transmission loss responses show a good agreement with the numerical results. The SMS-based edge filter used in the experiment is found to be suitable for use in a wavelength measurement system. Overall, it is shown that an SMS structure fabricated using a fusion splicer with three-axis adjustment has the advantage of a useful fabrication tolerance, within which the lateral misalignment has no significant effect on the slope of edge filter.

REFERENCES

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