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## Deactivation Effects of Tb<sup>3+</sup> on Ho<sup>3+</sup> Emission in Fluoroindate Glasses for 3.9 μm Laser Applications

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# Deactivation effects of $Tb^{3+}$ on $Ho^{3+}$ emission in fluorindate glasses for 3.9 $\mu m$ laser applications

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## **Abstract**

A series of  $Ho^{3+}/Tb^{3+}$  co-doped fluorindate glasses with good thermal stability have been synthesized to study the deactivation effects of  $Tb^{3+}$  on the  $Ho^{3+}$ : 3.9  $\mu m$  emission. Efficient 3.9  $\mu m$  emission enhancement is obtained under excitation by an 888 nm laser diode (LD). The Judd-Ofelt (J-O) intensity parameters and radiative properties are calculated to evaluate the spectroscopic properties. Possible energy transfer processes resulting in emission reinforcement are discussed. A higher spontaneous transition probability and larger peak emission cross section are achieved with the inclusion of  $Tb^{3+}$ . This analysis supports the conclusion that  $Ho^{3+}/Tb^{3+}$  co-doped fluorindate glass is a potentially useful laser material for highly efficient 3.9  $\mu m$  fiber lasers.

## **1. Introduction**

As the 3-5  $\mu\text{m}$  region overlaps with several common characteristic absorption wavelengths of gas molecules and possesses extremely high atmospheric transmittance, lasers operating in the 3-5  $\mu\text{m}$  region are of great interest in an increasing number of applications including gas monitoring, remote sensing, medical treatment and advanced radars [1-5]. To satisfy the need of laser sources for these applications, rare-earth (RE) doped fiber lasers have been considered as attractive candidates [6, 7], as they offer potential advantages including improved beam quality, robustness and high average output power [8]. The maximum average output power reported to date for fiber lasers operating at 3  $\mu\text{m}$  and 3.5  $\mu\text{m}$  are 70 W and 15 W, respectively [9, 10]. Compared to fiber lasers operating in the region 3-3.5  $\mu\text{m}$ , there has been little research carried out on 3.9  $\mu\text{m}$  fiber laser emission generated by the transition of  $\text{Ho}^{3+}$ :  ${}^5\text{I}_5 \rightarrow {}^5\text{I}_6$ , although fluoride fiber lasers have provided the longest wavelength [11, 12]. In 1997, by employing a pump wavelength at 890 nm and improved resonator cavity, lasing at 3.9  $\mu\text{m}$  was achieved and an improved average output power of 11 mW was demonstrated [13, 14]. However, it still required a cooling environment as the multi-phonon decay of  $\text{Ho}^{3+}$  ions in ZBLAN( $\text{ZrF}_4\text{-BaF}_2\text{-LaF}_3\text{-AlF}_3\text{-NaF}$ ) fiber generated a significant excess heat. The principal reasons for low output power in ZBLAN fibers are the high intrinsic phonon energy of ZBLAN glass and the self-termination effect of the  $\text{Ho}^{3+}$ :  ${}^5\text{I}_5 \rightarrow {}^5\text{I}_6$  transition [15]. To solve the first problem, fluoroindate glass has been considered, as it provides a lower phonon energy and a broader transmission window compared to

ZBLAN glass [16]. This glass has been successfully drawn into low-loss fibers and is useful for broadband supercontinuum generation and mid-infrared fiber lasing [17-20].

The self-termination effect of the  $\text{Ho}^{3+}: {}^5\text{I}_5 \rightarrow {}^5\text{I}_6$  transition, in similar manner to the transition of  $\text{Er}^{3+}: {}^4\text{I}_{9/2} \rightarrow {}^4\text{I}_{11/2}$  [21], results from the fact that the lifetime of the upper state  ${}^5\text{I}_5$  is much shorter than that of the lower state  ${}^5\text{I}_6$  [22]. In 2018, an output power of 200 mW with a slope efficiency of 10.2% at room temperature was obtained at 3.92  $\mu\text{m}$  in a cladding-pumped  $\text{Ho}^{3+}$ -doped fluoroindate fiber laser [23]. To suppress the self-termination effect, heavily  $\text{Ho}^{3+}$ -doped fluoroindate fiber was used to deplete the  ${}^5\text{I}_6$  state through the energy transfer up-conversion (ETU) process ( ${}^5\text{I}_6 + {}^5\text{I}_6 \rightarrow {}^5\text{F}_5 + {}^5\text{I}_8$ ).

In addition to the above approaches, energy transfer processes between RE ions have been investigated to deactivate the undesired long-lifetime of a lower laser state. In 2019, Li et al. demonstrated that the energy transfer from  $\text{Er}^{3+}: {}^4\text{I}_{13/2}$  to  $\text{Eu}^{3+}: {}^7\text{F}_6$  enhanced the 2.75  $\mu\text{m}$  emission in  $\text{Er}^{3+}/\text{Eu}^{3+}$  doped  $\text{PbF}_2$  crystals [24]. In 2020, the sensitization and deactivation effects of  $\text{Nd}^{3+}$  on the lower state of  $\text{Ho}^{3+}: {}^5\text{I}_6$  were investigated in fluoroindate glasses [25]. Yet, appropriate RE ions that can improve the luminescence efficiency of the  $\text{Ho}^{3+}: {}^5\text{I}_5 \rightarrow {}^5\text{I}_6$  transition are still under investigation.

In this work, we report the investigation of the luminescence properties and energy transfer mechanisms of  $\text{Ho}^{3+}$ -doped and  $\text{Ho}^{3+}/\text{Tb}^{3+}$ -co-doped fluoroindate glasses to identify the effects on the 3.9  $\mu\text{m}$  emission of this co-doping system. The emission spectra and fluorescence decay properties have been measured, and Judd-Ofelt parameters have been calculated. The above optical properties have been assessed to

demonstrate the feasibility of Ho<sup>3+</sup>/Tb<sup>3+</sup>-codoped fluorindate glasses for future applications in 3.9 μm fiber-lasers.

## 2. Experiment

The molar compositions of glass samples used in this investigation were (30.5-x)InF<sub>3</sub>-20ZnF<sub>2</sub>-20SrF<sub>2</sub>-16BaF<sub>2</sub>-6GaF<sub>3</sub>-6CaF<sub>2</sub>-1.5HoF<sub>3</sub>-xTbF<sub>3</sub>, where x=0, 0.1, 0.2, 0.3, 0.4, 0.5. These glasses were named as 1.5Ho-xTb. By employing a traditional melt quenching procedure [26], all chemicals were mixed from high purity (99.99%) raw materials. To avoid excessive water in the glass, all processes were carried out in a glove box filled with dry nitrogen. The prepared materials were completely melted in a Pt-Au crucible at 900 °C for 2 h, then annealed at 280 °C for a further 3 h, and finally naturally cooled down to room temperature to remove internal stress. The glasses were then polished for subsequent tests.

The experimental absorption spectra were measured by a Perkin-Elmer Lambda 750 UV-VIS-NIR spectrophotometer, while transmission spectra were measured using a Perkin-Elmer FTIR spectrometer. The infrared fluorescence spectra were tested using an Edinburg FLS1000 spectrometer. Differential scanning calorimetry (DSC) was analyzed using a NETZSCH DSC 204 F1 calorimeter. In the fluorescence lifetime test, the glass samples were excited employing a modulated Surelite OPO pulsed laser. Each measurement was performed at room temperature.

## 3. Result and Discussion

### 3.1 Vibrational characteristic and thermal stability

The Raman spectra of fluorindate glass with gaussian fit was shown in Figure 1. The bands centered at  $207\text{ cm}^{-1}$  is probably the bending modes of Ho-F and Tb-F together with asymmetric Zn-F and Ba-F stretching vibrations [27], previously reported in fluorozirconate glasses [28]. The band at  $421\text{ cm}^{-1}$  and  $507\text{ cm}^{-1}$  are in relation to symmetric stretching vibrations of bridge fluorine atoms of In-F<sub>b</sub>-In and non-bridged (nb) fluorine atoms F<sub>nb</sub>-In-F<sub>nb</sub> in octahedrons [InF<sub>6</sub>] [29]. The  $618\text{ cm}^{-1}$  band is on account of symmetrical stretching vibrations of non-bridged fluorine atoms in [GaF<sub>4</sub>] tetrahedrons [30, 31].

The DSC curve of the glass sample was measured for characteristic temperatures, including the glass transition temperature  $T_g$  and the crystallization temperature  $T_x$ , as shown in inset of Fig. 2(a). The evaluated  $\Delta T(T_x - T_g)$  of the fluorindate glass in our work is  $79.1\text{ }^\circ\text{C}$ , indicating that this particular composition has good thermal stability against crystallization during the fiber-fabrication process [32] and thus is a promising glass material for low-loss fibers [33].

### 3.2 Absorption spectra, and Judd-Ofelt analysis

The refractive index and density values for the fluorindate glass are 1.493 and  $5.134\text{ g/cm}^3$ , respectively. Figure 2(b) shows the absorption spectra of the samples in the wavelength range of 400-2400 nm at room temperature. The strong absorption band of Ho<sup>3+</sup>: <sup>5</sup>I<sub>5</sub> in the wavelength range 880-920 nm suggests that the Ho<sup>3+</sup> ions of glasses can be directly excited by an 888 nm LD. The transmission spectra of fluorindate glass

within the 1500-12000 nm wavelength range is shown in the inset of Fig. 2(a). It is worth noting that the glass samples exhibit excellent transmittance (more than 90%) over the wavelength range 1500-7000 nm, with an infrared cutoff wavelength of approximately 12000 nm. Furthermore, the calculated absorption associated to OH ( $\alpha_{OH}$ ) is as little as 0.23 ppm in a bulk glass 1 cm long [34], indicating that the undesirable energy transfer from  $Ho^{3+}$  to  $OH^-$  is very weak and consequently has little effect on the mid-IR emission [35].

The spectroscopic parameters  $\Omega_2$ ,  $\Omega_4$ ,  $\Omega_6$  of  $Ho^{3+}$  in the glasses are calculated using the Judd-Ofelt theory [36, 37] and the measured absorption spectra. Table 1 shows a comparison of spectroscopic parameters in various glasses. As expected, the  $\Omega_2$  in the  $Ho^{3+}/Tb^{3+}$  co-doped sample is higher than that in  $Ho^{3+}$  single doped sample, indicating that a lower symmetry and higher covalency for surrounding  $Ho^{3+}$  ions are generated by the introduction of  $Tb^{3+}$  ions [38, 39]. In contrast, the parameters  $\Omega_4$  and  $\Omega_6$  are associated with the viscosity and rigidity of the glass host [40]. The grown spectroscopic quality factor  $\Omega_4/\Omega_6$  in this case denotes that additive deactivated  $Tb^{3+}$  ions favor the energy transfer process  $Ho^{3+}: ^5I_5 \rightarrow ^5I_6$  [41].

Table 2 lists the calculated radiative parameters of the various transitions among corresponding energy levels of  $Ho^{3+}$  ions in the foundation of the acquired J-O intensity parameters [42]. The value of A of the  $Ho^{3+}: ^5I_5 \rightarrow ^5I_6$  transition in the  $Ho^{3+}/Tb^{3+}$  co-doped fluoroindate glass is calculated to be  $5.70 s^{-1}$ , which is larger than that in the  $Ho^{3+}$  single doped fluoroindate glass ( $5.02 s^{-1}$ ) and in the ZBYA glass ( $2.96 s^{-1}$ ) [43],



suggesting that the introduction of  $Tb^{3+}$  ions is advantageous to the  $Ho^{3+}$ : 3.9  $\mu m$  fluorescence emission efficiency in fluorindate glass.

### 3.3 Infrared fluorescence properties and energy transfer mechanism

Figure 3 and 4 show the MIR and NIR fluorescence spectra of  $Ho^{3+}$  doped and  $Ho^{3+}/Tb^{3+}$  co-doped glasses, resulting from the  $^5I_5 \rightarrow ^5I_6$ ,  $^5I_6 \rightarrow ^5I_7$ ,  $^5I_7 \rightarrow ^5I_8$ ,  $^5I_5 \rightarrow ^5I_7$ ,  $^5I_6 \rightarrow ^5I_8$  transitions of  $Ho^{3+}$ . Under the excitation of an 888 nm LD, the emission intensity at 3.9  $\mu m$  is increased by  $\sim 30\%$  after the inclusion of  $Tb^{3+}$ , indicating that  $^5I_6$  level has been depopulated by the introduced  $Tb^{3+}$ , resulting in an enhanced 3.9  $\mu m$  emission. The emission spectra have a full width at half maximum (FWHM) of 97 nm, which is similar to that of ZBYA glass [43]. It is worth mentioning that concentration quenching of the 3.9  $\mu m$  emission does not appear until the  $Tb^{3+}$  concentration reaches 0.3 mol.%. Concentration quenching may be caused by the increased proximity of  $Ho^{3+}$  and  $Tb^{3+}$  ions resulting from the increased concentration of  $Tb^{3+}$ . Fig. 4(c) shows that a similar effect has been observed also in the 1.7  $\mu m$  emission, indicating the deactivation effects of  $Tb^{3+}$  acts on the energy transfer of  $^5I_5 \rightarrow ^5I_7$ . Furthermore, Fig. 4 shows that other emissions with peak wavelengths located at 1.2  $\mu m$ , 2.0  $\mu m$  and 2.9  $\mu m$  exhibit a uniform declining tendency due to the depopulation of  $^5I_6$  and  $^5I_7$  states caused by the possible energy transfer between  $Ho^{3+}$  and  $Tb^{3+}$  ions.

Based on the above results, a possible energy transfer mechanism schematic for the  $Ho^{3+}/Tb^{3+}$  system under the excitation of an 888 nm LD is described in Fig. 5. Firstly,  $Ho^{3+}$  ions are excited to the upper state  $^5I_5$  from  $^5I_8$  by ground state absorption (GSA). After the

introduction of  $Tb^{3+}$  ions, a portion of the  $Ho^{3+}$  ions on the  $^5I_6$  state transfer energy to the adjacent  $Tb^{3+}: ^7F_0$  level via the ET1 process. Similarly, energy transmission takes place on account of the ET2 process between  $Ho^{3+}: ^5I_7$  and  $Tb^{3+}: ^7F_2$ . Furthermore, the cross-relaxation (CR1) process:  $Ho^{3+}: ^5I_6 + Tb^{3+}: ^7F_6 \rightarrow Ho^{3+}: ^5I_7 + Tb^{3+}: ^7F_4$  also quenches the lower state  $^5I_6$  to enhance the 3.9  $\mu m$  emission. The above processes work together to reduce the population of  $^5I_6$ , and thus enhance population inversion for the  $Ho^{3+}: ^5I_5 \rightarrow ^5I_6$  transition.

### 3.4 Fluorescence decay curves and calculated cross section

To further investigate the energy interaction mechanism between donor  $Ho^{3+}$  and acceptor  $Tb^{3+}$  ions, the fluorescence decay curves of the  $Ho^{3+}: ^5I_5$  and  $Ho^{3+}: ^5I_6$  energy levels of  $Ho^{3+}/Tb^{3+}$  co-doped and  $Ho^{3+}$  singly doped samples were measured under the excitation of an 888 nm pulsed laser, as shown in Fig. 6. The lifetime of the  $^5I_5$  level does not show any significant change after the inclusion of  $Tb^{3+}$ . On the contrary, the lifetime of both lower levels  $^5I_6$  and  $^5I_7$  exhibit a gradually decreasing tendency as the  $Tb^{3+}$  concentration increases. According to the ET processes described above, the lifetime of the  $^5I_6$  level in the  $Ho^{3+}/Tb^{3+}$  co-doped glasses (0.66 ms) is much shorter than that in the  $Ho^{3+}$  singly doped glass (3.86 ms). The quantum efficiency of ET between  $Ho^{3+}$  and  $Tb^{3+}$  was calculated using the following equation [39]:  $\eta = 1 - \tau_{Ho/Tb} / \tau_{Ho}$ , where  $\tau_{Ho}$  and  $\tau_{Ho/Tb}$  are the lifetimes of  $^5I_6$  state of  $Ho^{3+}$ -doped and  $Ho^{3+}/Tb^{3+}$  co-doped fluoroindate glasses, respectively. The quantum efficiency of ET is calculated to be 61.6% and the results confirm that  $Tb^{3+}$  can be used as an effective deactivation ion to depopulate  $Ho^{3+}: ^5I_6$  and enhance emission at 3.9  $\mu m$ .

In order to assess the gain properties for emission at 3.9  $\mu\text{m}$ , the emission cross-sections were calculated using the following Fuchtbauer-Ladenburg equation [44]:

$$\sigma_{emi} = \frac{\lambda^4 A_{rad}}{8\pi cn^2} \times \frac{\lambda I(\lambda)}{\int \lambda I(\lambda) d\lambda} \quad (1)$$

where  $\lambda$  is the wavelength.  $A_{rad}$  is the spontaneous transition probability and  $I(\lambda)$  is the measured fluorescence intensity at wavelength  $\lambda$ . Additionally,  $n$  and  $c$  are the refractive index and speed of light in a vacuum, respectively.

The absorption cross-sectional area  $\sigma_{abs}$  can be derived from by  $\sigma_{emi}$  using McCumber theory [45]:

$$\sigma_{abs} = \sigma_{emi} \times \left( \frac{Z_u}{Z_l} \right) \times \left[ \frac{-(E_{ul} - \hbar c \lambda^{-1})}{kT} \right] \quad (2)$$

In this formula,  $\hbar$  is Planck's constant,  $k$  is Boltzmann's constant,  $T$  is the temperature,  $E_{ul}$  is the energy gap between the ground state level and the excitation level and  $Z_u$ ,  $Z_l$  denote the partition functions of the upper and lower states, respectively. The maximum emission cross section in the  $\text{Ho}^{3+}/\text{Tb}^{3+}$  co-doped glass was calculated to be  $6.53 \times 10^{-21} \text{ cm}^2$  at 3930 nm, significantly higher than that ( $5.71 \times 10^{-21} \text{ cm}^2$ ) in the  $\text{Ho}^{3+}$  doped glass, as shown in Fig. 7. This suggests that the participation of  $\text{Tb}^{3+}$  ions will significantly increase the possibility of lasing at 3.9  $\mu\text{m}$ .

### 3.5 Population densities

To investigate the effect of co-doping with  $\text{Tb}^{3+}$  on population densities, a series of rate equations for 888 nm pumping were established, based on the model shown in Fig.

5. The small contribution of up-conversion is neglected to simplify the rate equations.

The rate equations thus are given by

$$\frac{dn_4}{dt} = \sigma_{14}\phi n_1 - \left( \frac{1}{\tau_4} + W_{mpr4} + C_{45}n_5 \right) n_4 \quad (3)$$

$$\frac{dn_3}{dt} = - \left( \frac{1}{\tau_3} + W_{mpr3} + C_{35}n_5 + W_{ET1}n_5 \right) n_3 + \left( \frac{1}{\tau_4} \beta_{43} + W_{mpr4} + C_{45}n_5 \right) n_4 \quad (4)$$

$$\frac{dn_2}{dt} = - \left( \frac{1}{\tau_2} + W_{ET2}n_5 \right) n_2 + \left( \frac{1}{\tau_3} \beta_{32} + W_{mpr3} + C_{35}n_5 \right) n_3 + \frac{1}{\tau_4} \beta_{42} n_4 \quad (5)$$

$$\frac{dn_1}{dt} = -\sigma_{14}\phi n_1 + \frac{1}{\tau_2} n_2 + \frac{1}{\tau_3} \beta_{31} n_3 + \frac{1}{\tau_4} \beta_{41} n_4 \quad (6)$$

where  $n_i$  is the population of the  $i$  level as illustrated in Fig. 4 ( $n_1+n_2+n_3+n_4+n_5 = 3.12 \times 10^{20} \text{ cm}^{-3}$ ).  $\sigma_{14}$  is the ground state absorption cross section (from  $\text{Ho}^{3+}: ^5\text{I}_8$  to  $\text{Ho}^{3+}: ^5\text{I}_5$ ).  $W_{mpr_i}$  and  $\tau_i$  are the multi-phonon relaxation rate and the radiative lifetime of the  $i$  level, respectively.  $C_{35}$  and  $C_{45}$  are the cross relaxation coefficients of CR1 and CR2 ( $\text{Ho}^{3+}: ^5\text{I}_5 + \text{Tb}^{3+}: ^7\text{F}_6 \rightarrow \text{Ho}^{3+}: ^5\text{I}_6 + \text{Tb}^{3+}: ^7\text{F}_5$ ), respectively.  $W_{ET1}$  and  $W_{ET2}$  are the energy transfer rates of ET1 and ET2.  $\beta_{ij}$  is the calculated branching ratio of the energy transition from  $i$  level to  $j$  level. The pump flux  $\phi$  is obtained from:

$$\phi = \frac{H\lambda}{\hbar c} \quad (7)$$

where  $H$  is the pump power density ( $1.59 \times 10^5 \text{ W/m}^2$ ) and  $\lambda$  is the pump light wavelength (888 nm).  $\hbar$  and  $c$  are the Planck constant and light speed in a vacuum, respectively.

Based on the above equations, the steady-state population of the  $^5\text{I}_5$  level was performed using [46]:

$$n_4 = \frac{\sigma_{14}\phi n_1}{\frac{1}{\tau_4} + W_{mpr4} + C_{45}n_5} \quad (8)$$

To simplify the calculation process, the populations of the ground state of  $\text{Ho}^{3+}$  ( $n_1$ ) and  $\text{Tb}^{3+}$  ( $n_5$ ) are assumed to be equal to the doping concentration of  $\text{Ho}^{3+}$  and  $\text{Tb}^{3+}$ , respectively.  $W_{mpr4}$  and  $C_{45}$  can be calculated from:

$$\frac{1}{\tau_{m4}} = \frac{1}{\tau_{r4}} + W_{mpr4} + C_{45}n_5 \quad (9)$$

where  $\tau_{m4}$  and  $\tau_{r4}$  are the measured and calculated radiative lifetime of the  ${}^5\text{I}_5$  level, respectively. Therefore, the dependence of  $n_4$  on concentrations can be calculated. The populations of the  ${}^5\text{I}_6$  level ( $n_3$ ) is obtained by [47]:

$$\frac{n_4}{n_3} = \left( \frac{A_3}{\beta_{43}A_4} \right) \frac{\int \lambda I_{3.9\mu\text{m}}(\lambda) d\lambda}{\int \lambda I_{1.2\mu\text{m}}(\lambda) d\lambda} \quad (10)$$

where  $A_3$  and  $A_4$  are the calculated radiative transition probabilities of the  ${}^5\text{I}_6$  and  ${}^5\text{I}_5$  levels, respectively. Figure 8 shows the population densities of the two levels for different  $\text{Tb}^{3+}$  concentrations calculated from the equations above. For increasing  $\text{Tb}^{3+}$  concentration, the calculated population of  ${}^5\text{I}_5$  rises slightly due to the larger absorption cross section of  ${}^5\text{I}_8 \rightarrow {}^5\text{I}_5$ , while that of the lower level  ${}^5\text{I}_6$  drops substantially because of the ET processes proposed.

#### 4. Conclusion

In conclusion,  $\text{Ho}^{3+}$  doped and  $\text{Ho}^{3+}/\text{Tb}^{3+}$  co-doped fluoroindate glasses have been fabricated. The introduction of  $\text{Tb}^{3+}$  resulted in a high spontaneous transition probability and large emission cross section. Compared to the  $\text{Ho}^{3+}$  doped sample, enhanced 3.9  $\mu\text{m}$

emission was obtained under excitation by an 888 nm LD. An energy transfer mechanism explained how  $Tb^{3+}$  exerted a positive effect on the population inversion of the  ${}^5I_5 \rightarrow {}^5I_6$  transition. These achievements show that  $Ho^{3+}/Tb^{3+}$  co-doped fluorindate glasses could be promising materials for a 3.9  $\mu m$  fiber lasers.

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## Figure Captures

**Fig. 1.** Gaussian fit peaks of Raman spectrum in the fluoroindate glass.

**Fig. 2.** (a) Transmission spectrum of 1.5 mol.%  $\text{Ho}^{3+}$ -doped glass; (b) absorption spectra of 1.5 mol.%  $\text{Ho}^{3+}$ , 3 mol.%  $\text{Tb}^{3+}$  singly doped and  $\text{Ho}^{3+}/\text{Tb}^{3+}$  codoped glasses. Inset: differential scanning calorimetry curve in the temperature range 200-500 °C and photograph of glass samples.

**Fig. 3.** Emission spectra of  $\text{Ho}^{3+}$  single-doped and  $\text{Ho}^{3+}/\text{Tb}^{3+}$  co-doped glasses in the wavelength region 3650-4200 nm. Inset: dependence of the luminescence intensity on the concentration of  $\text{Tb}^{3+}$  ions.

**Fig. 4.** Fluorescence spectra of  $\text{Ho}^{3+}$  single-doped and  $\text{Ho}^{3+}/\text{Tb}^{3+}$  co-doped fluoroindate glasses in the wavelength region (a) 2600-3200 nm; (b) 1800-2200 nm; (c) 1550-1800 nm; and (d) 1100-1280 nm.

**Fig. 5.** Energy level diagram and energy transfer process between  $\text{Ho}^{3+}$  and  $\text{Tb}^{3+}$  under 888 nm LD excitation.

**Fig. 6.** Luminescence decay curves of (a) the  $^5I_5$  and (b) the  $^5I_6$  energy levels; (c) experimental lifetimes of  $^5I_5$  and  $^5I_6$  levels; (d) measured lifetime of the  $^5I_7$  level and the dependence of the  $^5I_5$  to  $^5I_6$  lifetime ratio for different  $Tb^{3+}$  concentrations.

**Fig. 7.** Absorption and emission cross-sections corresponding to  $^5I_5 \rightarrow ^5I_6$  transitions of  $Ho^{3+}$  in single-doped (solid line) and  $Ho^{3+}/Tb^{3+}$  co-doped (dash line) fluorindate glasses.

**Fig. 8.** Population densities of  $^5I_5$  and  $^5I_6$  levels in glasses with different  $Tb^{3+}$  concentration.

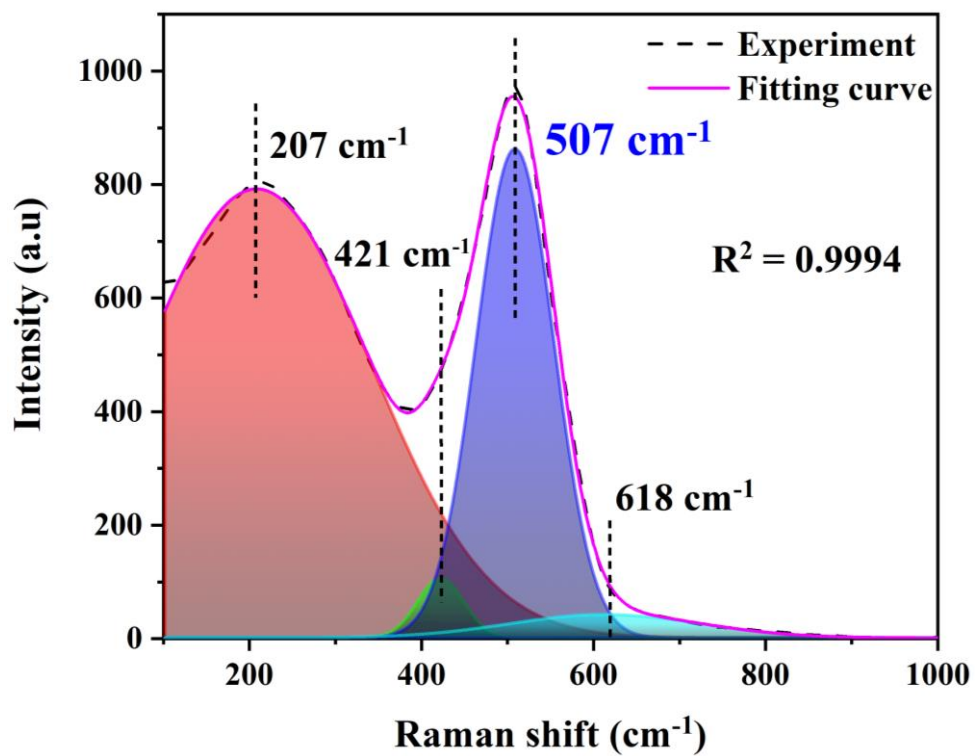
**Table 1.** J-O parameters of  $\text{Ho}^{3+}$  in various glasses.

Glass Sample	$\Omega_2$	$\Omega_4$	$\Omega_6$	Reference
1.5Ho	1.06	2.13	1.99	This work
1.5Ho-0.3Tb	1.10	2.50	2.24	
ZBYA	3.89	2.52	0.54	[43]

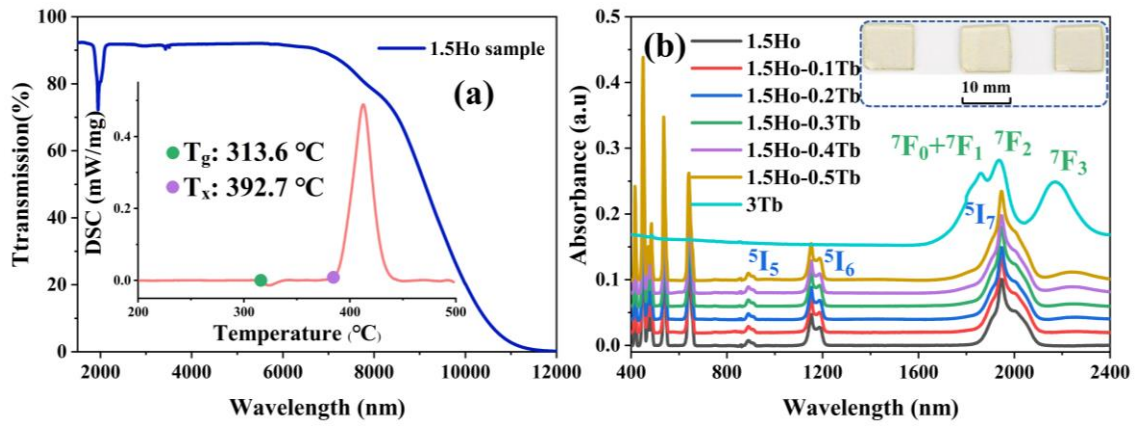
**Table 2.** Calculated Spontaneous Transition Probability( $A$ ), Branching Ratios ( $\beta$ ) and Radiative Life Times ( $\tau_{\text{rad}}$ ) for various selected excited states of  $\text{Ho}^{3+}$  in singly doped and codoped samples.

Glass Sample	Transition	$\lambda$ (nm)	$A$ ( $\text{s}^{-1}$ )	$\beta$ (%)	$\tau_{\text{rad}}$ (ms)
1.5Ho	${}^5\text{I}_5 \rightarrow {}^5\text{I}_6$	3920	5.02	3.65	7.26
	$\rightarrow {}^5\text{I}_7$	1680	74.96	54.47	
	$\rightarrow {}^5\text{I}_8$	889	57.64	41.88	
	${}^5\text{I}_6 \rightarrow {}^5\text{I}_7$	2870	15.17	9.54	6.29
	$\rightarrow {}^5\text{I}_8$	1190	143.89	90.46	
	${}^5\text{I}_7 \rightarrow {}^5\text{I}_8$	2020	58.05	100	
1.5Ho-0.3Tb	${}^5\text{I}_5 \rightarrow {}^5\text{I}_6$	3920	5.70	3.67	6.44
	$\rightarrow {}^5\text{I}_7$	1680	84.46	54.38	
	$\rightarrow {}^5\text{I}_8$	889	65.16	41.95	
	${}^5\text{I}_6 \rightarrow {}^5\text{I}_7$	2870	17.15	9.56	5.57
	$\rightarrow {}^5\text{I}_8$	1190	162.26	90.44	
	${}^5\text{I}_7 \rightarrow {}^5\text{I}_8$	2020	65.54	100	

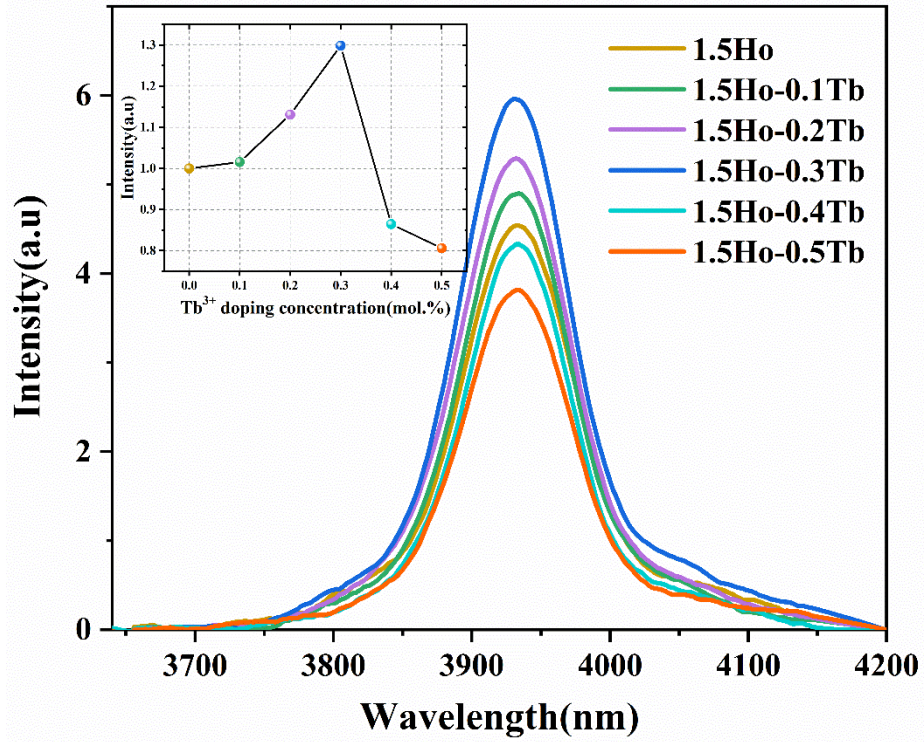




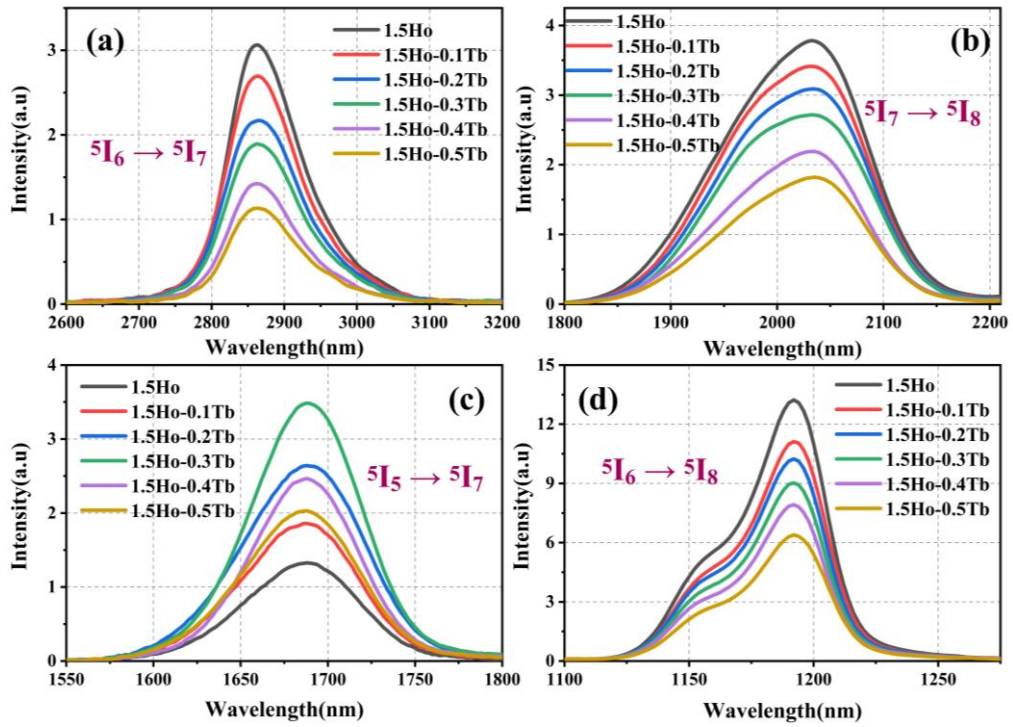
**Fig. 1.** Gaussian fit peaks of Raman spectrum in the fluorindate glass.



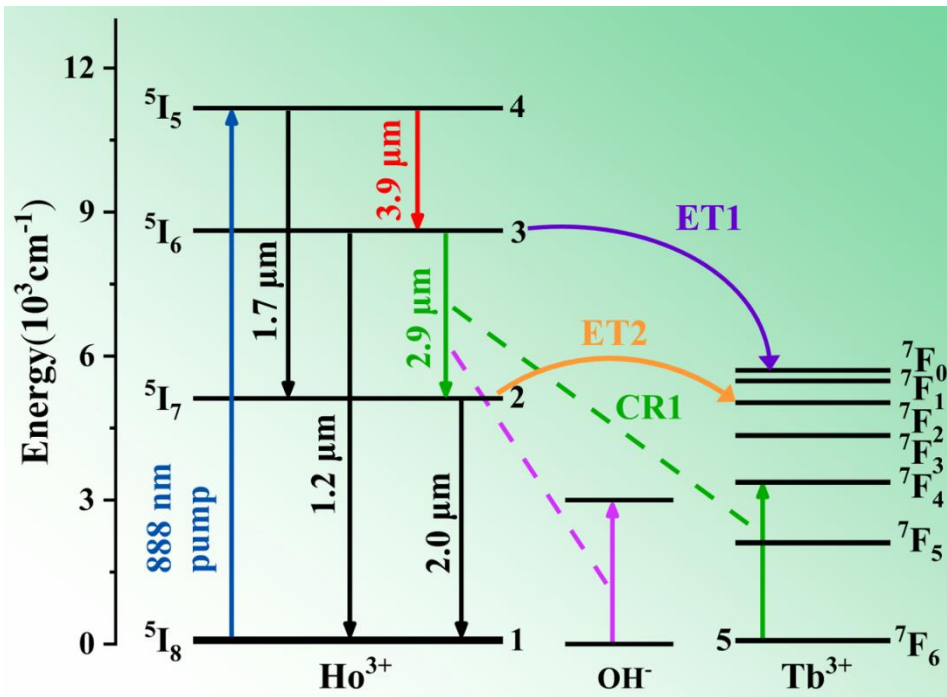
**Fig. 2.** (a) Transmission spectrum of 1.5 mol.% Ho<sup>3+</sup>-doped glass; (b) absorption spectra of 1.5 mol.% Ho<sup>3+</sup>, 3 mol.% Tb<sup>3+</sup> singly doped and Ho<sup>3+</sup>/ Tb<sup>3+</sup> codoped glasses. Inset: differential scanning calorimetry curve in the temperature range 200-500 °C and photograph of glass samples.



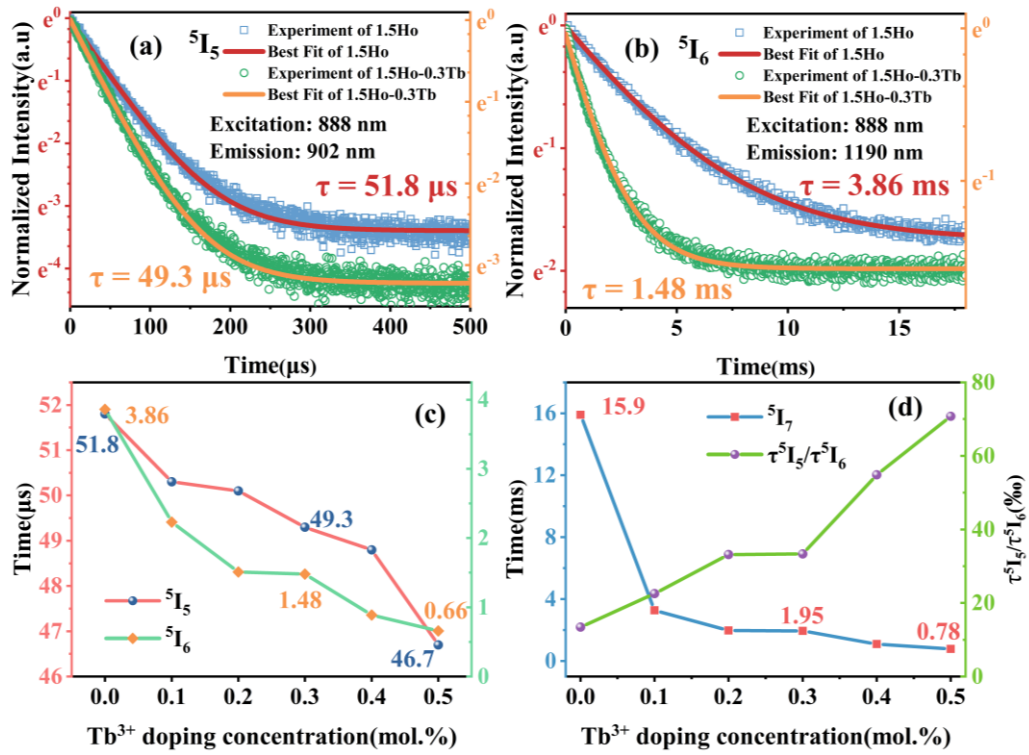
**Fig. 3.** Emission spectra of Ho<sup>3+</sup> single-doped and Ho<sup>3+</sup>/Tb<sup>3+</sup> co-doped glasses in the wavelength region 3650-4200 nm. Inset: dependence of the luminescence intensity on the concentration of Tb<sup>3+</sup> ions.



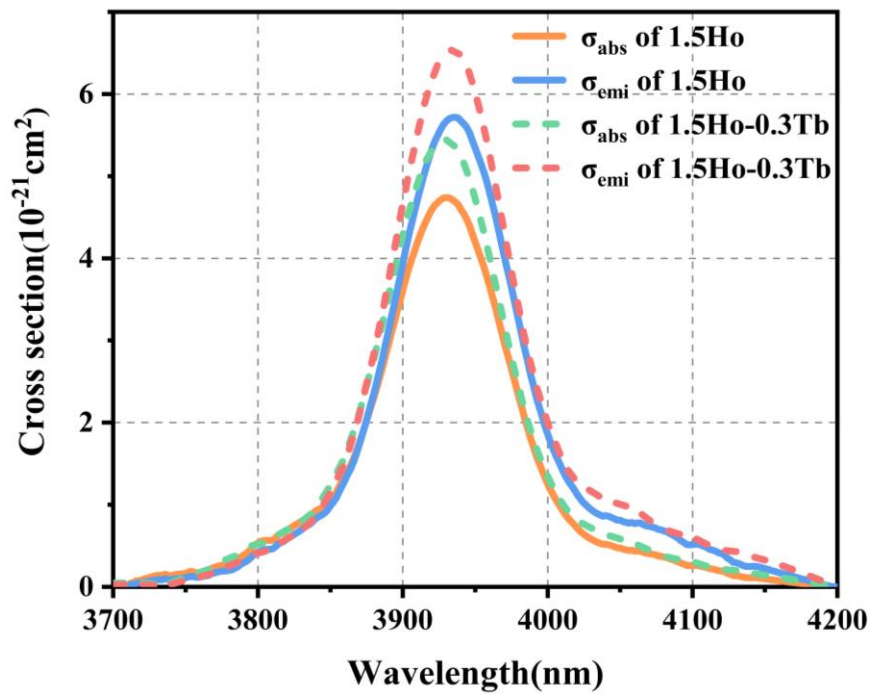
**Fig. 4.** Fluorescence spectra of Ho<sup>3+</sup> single-doped and Ho<sup>3+</sup>/Tb<sup>3+</sup> co-doped fluorindate glasses in the wavelength region (a)2600-3200 nm; (b)1800-2200 nm; (c) 1550-1800 nm; and (d)1100-1280 nm.



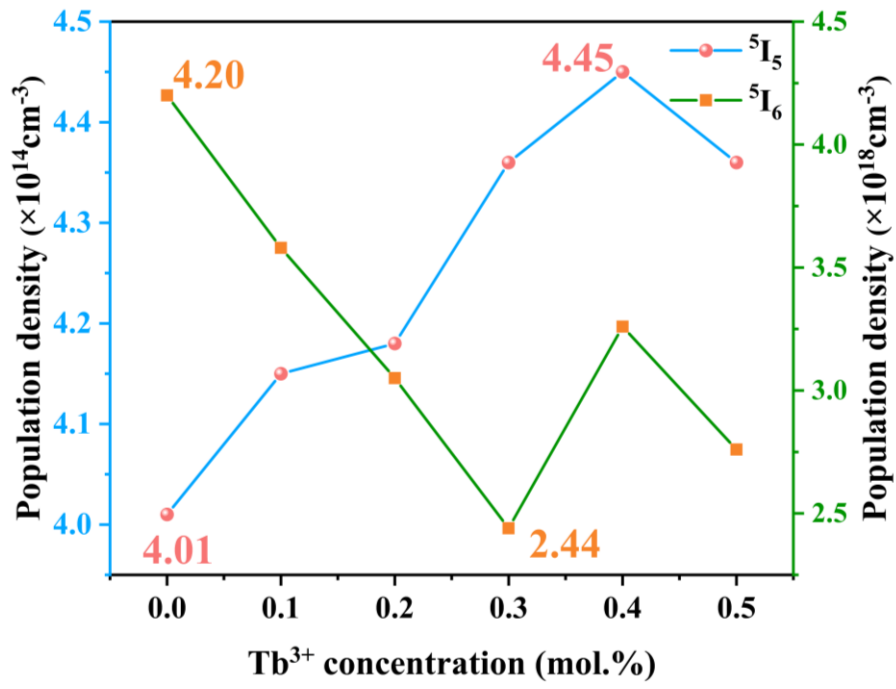
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