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## Relating Fractal Dimension to Branching Behaviour in Filamentous Microorganisms

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# Relating fractal dimension to branching behaviour in filamentous microorganisms

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**Abstract**—The productivity of an industrial fermentation process involving a filamentous microbe is heavily dependent on the morphological form adopted by the organism. The development of systems capable of rapidly and accurately characterising morphology within a given process represents a significant challenge to biotechnologists, as the complex phenotypes that are manifested are often not easily quantified. Conventional parameters employed in these analyses are of limited value, as they reveal little about the specific branching behaviour of the organism, which is an important consideration given the demonstrated link between branching frequency and metabolite production. More recently, fractal geometry has been employed in the analysis of microbes, but a clear link between fractal dimension and branching behaviour has not been demonstrated.

This study presents an alternative means of enumerating the fractal dimension of fungal mycelial structures, by generating a ‘fractal signal’ from an object boundary. In the analysis of a population of *Aspergillus oryzae* mycelia, both fractal dimension and hyphal growth unit were found to increase together over time. An extensive analysis of different populations of *Penicillium chrysogenum* and *A. oryzae* mycelia, cultivated under a variety of different conditions, revealed a strong correlation between fractal dimension and hyphal growth unit. The technique has the potential to be adapted and applied to any morphological form that may be encountered in a fermentation process, providing a universally applicable process parameter for more complete data acquisition.

**Index Terms**—Industrial Fermentations, Fractal Analysis, Fractal Signals, Filamentous Microorganisms, Morphological Quantification.

## I. INTRODUCTION

THE optimisation of industrial fermentation processes involving filamentous microorganisms requires an in-depth knowledge of the relationship between biomass and metabolite production. The specific morphological form adopted by an organism in a certain process, which is dependent on a variety of factors [1], is of critical importance to the clarification of this relationship, as particular phenotypes are associated with maximum productivity. The accurate quantification of phenotypic variation in vegetative mycelia, as a means of process control, is therefore of the utmost importance. With

the advent of image analysis systems, significant progress has been made in furthering the understanding of the relationship between morphology and productivity [2]. However, the accurate quantification of complex morphologies still represents a major challenge in process optimisation.

At the microscopic level, filamentous microorganisms consist of hyphae exhibiting strongly polarised growth that develop into a composite structure termed a mycelium, which is conventionally characterised based on the ratio of the total hyphal length to the number of branches formed. This measure, termed the hyphal growth unit ( $L_{HGU}$ ), was first proposed by Plomley [3] and is still a common means of morphological quantification [4], [5], [6], [7]. The growth unit effectively provides an overview of the branching behaviour of an organism under a given set of environmental conditions; a low value indicates a high rate of branch formation, whereas a high value is indicative of a relatively unbranched structure. The extent to which an organism forms branches is often of interest in industrial processes, as evidence in the literature suggests that metabolite excretion occurs primarily at hyphal tips [8], [9]. A knowledge of branching behaviour is therefore of significant interest in the design of a particular bioprocess.

At the macroscopic level, the dispersed mycelial morphological form may dominate, or an aggregation of biomass may result in mycelial ‘clumps’ being predominant. These clumps may develop into dense, approximately spherical structures termed ‘pellets’, which may be up to several millimetres in diameter (Fig. 1). In fermentations of certain microorganisms, such as *Aspergillus oryzae*, there is evidence that pellet-formation is driven by spore agglomeration [10] and, as such, the occurrence of ‘free’ mycelia may be rare. The characterisation of these complex macro-morphologies represents a far greater challenge to the fungal biotechnologist, as individual hyphae cannot be isolated and enumerated. As such, the accurate determination of the extent of branching of the organism is often impossible. These large aggregates of biomass are conventionally characterised in terms of projected area ( $A_p$ ), perimeter length ( $P$ ), circularity ( $C = 4\pi A_p P^{-2}$ ), or various other interpretations thereof [5], [11], [12]. As different morphological parameters are often utilised depending on the growth form present, a considerable amount of effort has been expended in designing imaging systems capable of discriminating between these different phenotypes [5], [11].

An alternative approach to morphological quantification employs the use of fractal geometry to characterise the spatial distribution of an organism. The term ‘fractal’ geometry was first used by Mandelbrot [13] to describe objects that are

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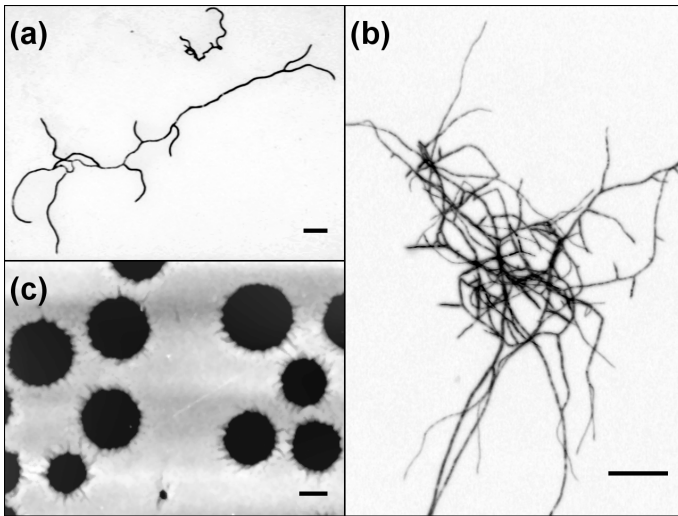


Fig. 1. Typical morphologies found in submerged fermentations of filamentous microorganisms: (a) Freely dispersed mycelia (Bar = 50 $\mu$ m) (b) Mycelial clump (Bar = 100 $\mu$ m) (c) Pellets (Bar = 2.5mm)

‘self-similar’ (similar at different scales). Several studies have since demonstrated that certain filamentous microorganisms can be considered self-similar structures [6], [14], [15], [16], [17], [18], [19], as do several bacterial strains of Gram-negative rods, under certain conditions [20]. Effects of different grazing densities of collembolans on colonies of the fungus *Hypholoma fasciculare* [21] and trophic responses of *Phanerochaete velutina* mycelial systems to nutrient stimuli [22] were also quantified in the same manner. Fractal geometry has also been used as a means of standardising mycelial inocula for submerged fermentations [23].

A number of techniques have been used for estimating the fractal dimension ( $D$ ), but the ‘box-counting’ method has been by far the most common in the analysis of filamentous microbes [24]. This approach entails covering the mycelium with a grid of side length  $\epsilon$  and counting the number of boxes,  $N(\epsilon)$ , that are intersected by the mycelium. If the mycelium is a true fractal, then a relationship of the following form should be found:

$$N(\epsilon) = c\epsilon^{-D}$$

where  $c$  is a proportionality constant. The fractal nature of mycelia has been studied at two distinct levels using the measures of the surface fractal dimension ( $D_{BS}$ ), effectively allowing discrimination between systems which are fractal only at their boundaries, and the mass fractal dimension ( $D_{BM}$ ). However, it has been suggested that the fractal dimension is often not sufficient for morphological characterisation, as microorganisms can sometimes appear to have different branching patterns, despite having similar values for fractal dimension [25].

While numerous studies have been conducted in which fractal analysis is utilised to quantify morphology, few have attempted to link fractal dimension with conventional morphological parameters. Fractal analysis is of significant potential value in the study of filamentous microorganisms, particularly

as it lends itself to the quantification of all gross morphological forms that may be encountered. However, there is a need to develop further the relationship between the fractal dimension within a population of mycelia and the branching behaviour within that population. Here we describe an alternative approach to fractal analysis, which directly relates the hyphal growth unit to the fractal dimension, based on an analysis of the mycelial boundary.

## II. MATERIALS & METHODS

*Penicillium chrysogenum* (IMI 321325) spores were harvested from malt agar (Lab M) slant cultures by addition of 5 ml phosphate-buffered saline (PBS; pH 7.2, Oxoid Dulbecco ‘A’; 0.85% w/v) containing Tween 80 (0.1% v/v). Conidiospores were dislodged using a sterile swab, briefly mixed, and the suspension was filtered through sterile glass wool to remove hyphae. The inoculum was standardized using a Neubauer chamber to yield a stock concentration of  $2 \times 10^6$  spores ml<sup>-1</sup>, glycerol added to a final concentration of 20% (v/v) and aliquots stored at -20°C. The viability of spores after freezing was found to be approximately 47% of stock concentration (pour plate method, malt agar, 36 h incubation). *Aspergillus oryzae* (ATTC 12891) inoculum preparation was as previously described [4].

The basal medium used for solid state fermentation of *A. oryzae* was a modification of that described by Amanullah and colleagues [26]: Citric Acid, 2.0g/L; MgSO<sub>4</sub>·7H<sub>2</sub>O, 2.0g/L; KH<sub>2</sub>PO<sub>4</sub>, 2.0g/L; (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub>, 3.0g/L; CaCl<sub>2</sub>·2H<sub>2</sub>O, 1.1g/L; K<sub>2</sub>SO<sub>4</sub>, 2.0g/L; Soluble Starch, 10.0g/L; Agar No. 1, 17.0g/L. A trace metal solution was added (0.5ml/L), consisting of: Citric acid, 3.0g/L; ZnSO<sub>4</sub>·7H<sub>2</sub>O, 0.5g/L; FeSO<sub>4</sub>·7H<sub>2</sub>O, 0.5g/L; CuSO<sub>4</sub>, 0.25g/L; MnSO<sub>4</sub>·H<sub>2</sub>O, 0.28g/L; NiCl<sub>2</sub>·6H<sub>2</sub>O, 0.09g/L. Nonidet P-40 or Triton X-100 were added to yield a final concentration of either 0.1% or 5.0% w/v. The media was adjusted to pH 6.0 before autoclaving at 121°C for 15 minutes. Solid state fermentation of *P. chrysogenum* was carried out using the following: malt agar, malt agar supplemented with CaCl<sub>2</sub>·2H<sub>2</sub>O (0.08% w/v) or FeCl<sub>2</sub>·4H<sub>2</sub>O (0.11% w/v), rice, orange and a mixture of rice and bulgar wheat (1:1 w/w). Rice and rice-bulgar wheat were prepared by steeping in water and autoclaving (121°C for 15 minutes) before transfer to sterile Petri dishes. Orange was prepared for use by surface swabbing with alcohol and dissection with a sterile knife. Cell immobilisation, cultivation conditions and processing of culture for image analysis were as previously described [4].

Submerged fermentation of *A. oryzae* was carried out in a 2L Benchtop Fermentor (BioFlo 110, New Brunswick Scientific). The approximate internal diameter of the vessel was 0.13m and it had a working volume of 1.5L. Agitation was provided by two Rushton turbines with a D/T ratio of 0.4 operated at 200 rpm. A pipe sparger was used to aerate the culture at an initial rate of 1.0 vvm. The fermentor was run without dissolved oxygen or pH control and the broth temperature was maintained at 30°C. Inoculum work-up consisted of three shake flask cultures (250ml, 20% working volume) inoculated with  $5 \times 10^7$  spores ml<sup>-1</sup> and incubated at 30°C (200rpm for 48 hours). The medium used for fermentation and

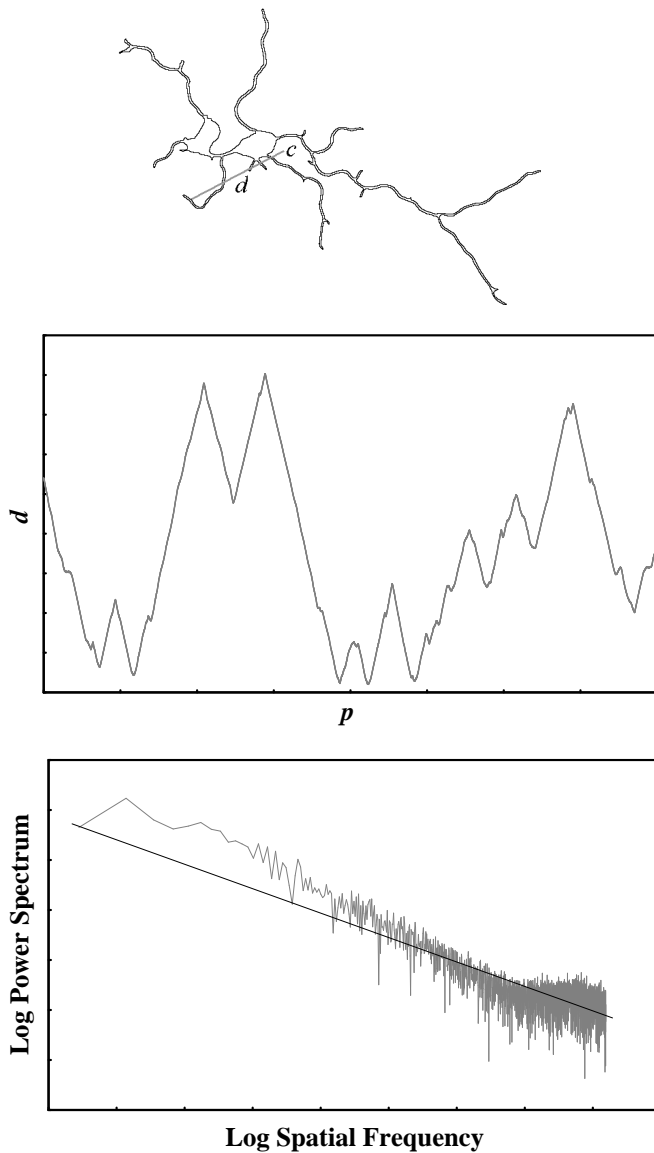


Fig. 2. Illustration of algorithm for determination of fractal dimension of mycelial structures. Distance,  $d$ , between the centroid,  $c$ , and the boundary is plotted for each position on the boundary,  $p$ , and the fractal dimension derived from a log-log plot of the fourier domain representation of the signal.

inoculum work-up was as described above (Agar No. 1 and detergents omitted). Samples taken for microscopic analysis were diluted approximately 1:50 with PBS-Tween 80 (0.1% w/v). The diluted sample (1ml) was added to 4ml of calcofluor white (0.01% w/v) and incubated at room temperature for 10 minutes, before filtration through a cellulose nitrate membrane (Sartorius Stedim 11306-47-ACN) and drying at 65°C (75 minutes).

Light microscopy and image capture were as previously described [4]. Images of submerged culture samples were captured with a Canon PowerShot S50 digital camera attached to a fluorescence microscope (Leitz Laborlux S) fitted with an epifluorescence illuminator (307-148.002 514687, Leitz Wetzlar). Images were captured at 100x magnification.

In all cases, only ‘free’ mycelial elements, exhibiting minimal overlapping of hyphae, were considered for image

analysis, so that comparisons could be drawn between the fractal dimension and the hyphal growth unit. The generation of binary images and the enumeration of the hyphal growth unit were as previously described [4]. The fractal dimension,  $D$ , of an object,  $O$ , was determined by first locating the object boundary in a binary image (all foreground pixels bordering background), which can be thought of as a ‘fractal curve’, consisting of a set of  $N$  coordinates,  $(x_n, y_n)$ . From this series of points, a ‘fractal signal’,  $f(n)$ , can be constructed as follows:

$$f(n) = \sqrt{(x_n - x_c)^2 + (y_n - y_c)^2} \text{ for all } 0 < n < N$$

where  $(x_c, y_c)$  is the average location of all  $(x, y) \in O$ . If  $f(n)$  is a fractal signal, then the following relationship holds true:

$$P(\omega) = \frac{c}{\omega^\beta}$$

where  $P(\omega) = |F(\omega)|^2$ ,  $F(\omega)$  is the Fourier transform of  $f(n)$ ,  $\beta = 2q$ ,  $q$  is the Fourier Dimension and  $c$  is a constant. Taking the log of this equation yields:

$$\ln(P(\omega)) = -\beta \ln(\omega) + c$$

$$D = \frac{5 - \beta}{2}$$

A value for  $\beta$  can therefore be determined by linear regression of a plot of  $\ln(P(\omega))$  against  $\ln(\omega)$  (Fig. 2). A more complete treatment of fractal curves and fractal signals can be found in the literature [27]. All algorithms were implemented in Java using ImageJ v1.41o (US National Institutes of Health).

### III. RESULTS & DISCUSSION

An analysis of the development of *A. oryzae* on malt agar showed that both  $D$  and  $L_{HGU}$  increased over time and both tended towards approximately constant values (Fig. 3). This suggests that the value of  $L_{HGU}$  specific to *A. oryzae* under these growth conditions is reflected in the fractal dimension

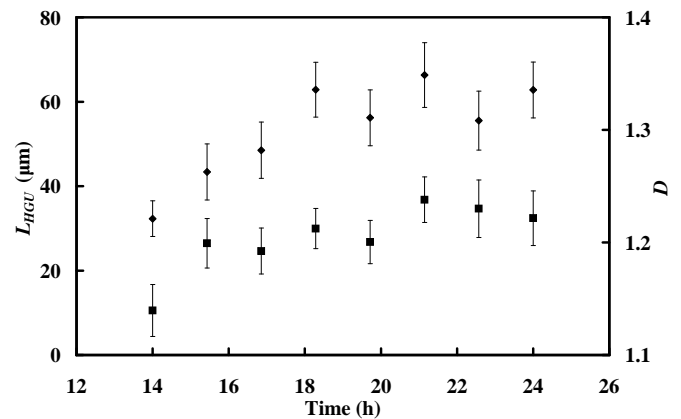


Fig. 3. Temporal variation in mean hyphal growth unit ( $L_{HGU}$ ; ◆) and the mean fractal dimension ( $D$ ; ■) of populations of *A. oryzae* cultivated on malt agar. Error bars represent 95% confidence intervals.

TABLE I  
POPULATIONS OF FILAMENTOUS FUNGI ANALYSED, WHERE  $n$  IS THE NUMBER OF MYCELIA IN EACH POPULATION AND THE TOTAL HYPHAL LENGTH IS PRESENTED AS MEAN  $\pm$  95% CONFIDENCE INTERVAL

Organism	Incubation Time (h)	Substrate	n	Total Hyphal Length ( $\mu\text{m}$ )
<i>A. oryzae</i>	14.0	Malt Agar <sup>1</sup>	86	85 $\pm$ 16
<i>A. oryzae</i>	15.4	Malt Agar	87	117 $\pm$ 21
<i>A. oryzae</i>	16.9	Malt Agar	82	169 $\pm$ 41
<i>A. oryzae</i>	18.3	Malt Agar	78	341 $\pm$ 71
<i>A. oryzae</i>	19.7	Malt Agar	83	305 $\pm$ 66
<i>A. oryzae</i>	21.1	Malt Agar	67	428 $\pm$ 98
<i>A. oryzae</i>	22.6	Malt Agar	59	336 $\pm$ 101
<i>A. oryzae</i>	24.0	Malt Agar	76	397 $\pm$ 91
<i>A. oryzae</i>	18.0	Solid medium, Nonidet P-40 5.0% (w/v)	30	190 $\pm$ 44
<i>A. oryzae</i>	24.0	Solid medium, Nonidet P-40 5.0% (w/v)	26	654 $\pm$ 177
<i>A. oryzae</i>	15.0	Solid medium, Triton X-100 0.1% (w/v)	44	177 $\pm$ 39
<i>A. oryzae</i>	18.0	Solid medium, Triton X-100 0.1% (w/v)	35	269 $\pm$ 95
<i>A. oryzae</i>	46.0	Submerged Medium	38	874 $\pm$ 198
<i>A. oryzae</i>	72.5	Submerged Medium	56	671 $\pm$ 116
<i>A. oryzae</i>	94.0	Submerged Medium	44	527 $\pm$ 126
<i>P. chrysogenum</i>	20.0	Malt Agar	69	116 $\pm$ 18
<i>P. chrysogenum</i>	27.0	Malt Agar	46	378 $\pm$ 73
<i>P. chrysogenum</i>	20.0	Malt Agar, CaCl <sub>2</sub> .2H <sub>2</sub> O 0.08% (w/v)	68	131 $\pm$ 20
<i>P. chrysogenum</i>	27.0	Malt Agar, CaCl <sub>2</sub> .2H <sub>2</sub> O 0.08% (w/v)	32	296 $\pm$ 52
<i>P. chrysogenum</i>	27.0	Malt Agar, FeCl <sub>2</sub> .4H <sub>2</sub> O 0.11% (w/v)	58	140 $\pm$ 26
<i>P. chrysogenum</i>	20.0	Orange	39	180 $\pm$ 36
<i>P. chrysogenum</i>	19.0	Rice	114	255 $\pm$ 31
<i>P. chrysogenum</i>	20.0	Rice & Bulgar Wheat	42	400 $\pm$ 121

<sup>1</sup> Results for *A. oryzae* on malt agar were produced using images generated during a previous study [4].

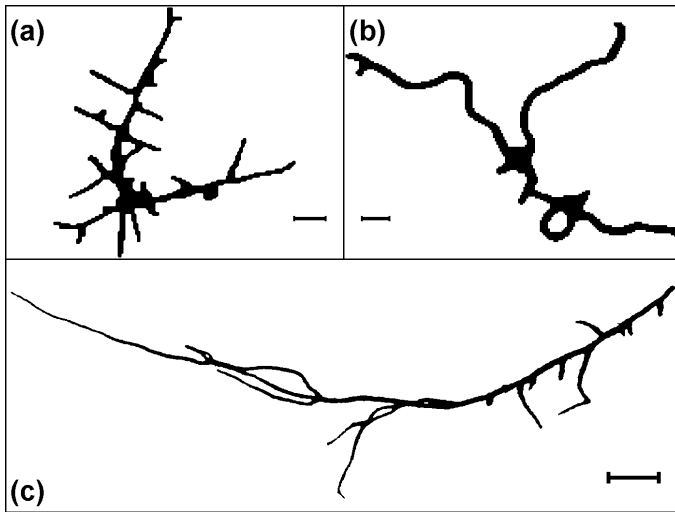


Fig. 4. Different morphological forms of filamentous fungi. (a) *Penicillium chrysogenum* 27 hours after inoculation on malt agar;  $D = 1.087$ ,  $L_{HGU} = 25.8\mu\text{m}$  (bar =  $20\mu\text{m}$ ). (b) *Aspergillus oryzae* 21 hours after inoculation on malt agar;  $D = 1.243$ ,  $L_{HGU} = 66.5\mu\text{m}$  (bar =  $20\mu\text{m}$ ). (c) *Aspergillus oryzae* 46 hours after inoculation in submerged culture;  $D = 1.271$ ,  $L_{HGU} = 121.0\mu\text{m}$  (bar =  $100\mu\text{m}$ ).

of the mycelia. The fractal dimension of *Ashbya gossypii* and *Streptomyces griseus* were also found to increase with time during the colonisation of solid substrates [24]. *A. oryzae* and *P. chrysogenum* were grown under a variety of different conditions (Table I), producing mycelia of varying size and dimension (Fig. 4) that were quantified in the same manner. The resultant mean values of  $D$  obtained for each population were plotted against the mean values of  $L_{HGU}$  to yield an approximately logarithmic relationship (Fig. 5):

$$D = a \ln(L_{HGU}) + b$$

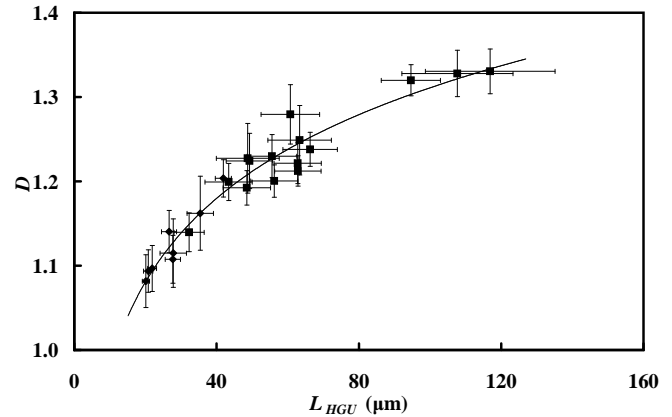


Fig. 5. Relationship between the mean hyphal growth unit ( $L_{HGU}$ ) and the mean fractal dimension ( $D$ ) of populations of *Aspergillus oryzae* (■) and *Penicillium chrysogenum* (◆) mycelia, grown under a variety of different conditions (Table I). A logarithmic relationship of the form  $D = a \ln(L_{HGU}) + b$  exists between the two parameters, where  $a = 0.14$  and  $b = 0.65$  (—;  $R^2 = 0.95$ ). Error bars represent 95% confidence intervals.

where  $a$  and  $b$  are constants. This result demonstrates a strong correlation between the branching behaviour of mycelia and their space-filling properties. However, it has been shown in other studies that fractal dimension tends to increase as projected area of mycelial structures increases [6]. This may also be the case in this study, as higher values of  $D$  tended to be biased toward high values of  $A_p$  (Fig. 6), but this result is inconclusive, as the sizes of mycelia analysed fell within a relatively small range.

This result demonstrates a clear relationship between the branching behaviour of filamentous organisms and the fractal dimension of the resultant mycelial structures, further emphasising the potential use of fractal analysis in morphological quantification. An ability to extract information on the

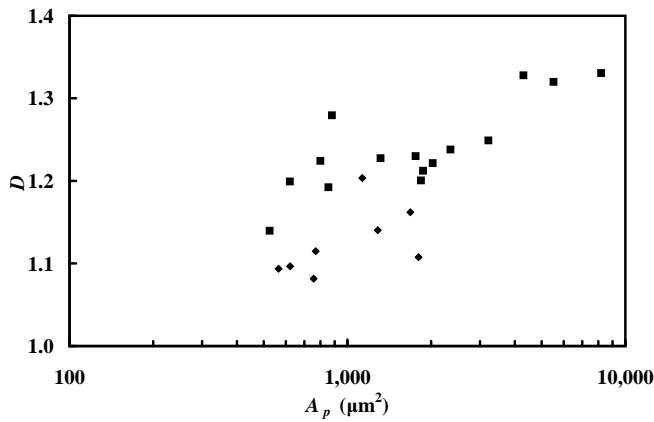


Fig. 6. Relationship between mean fractal dimension ( $D$ ) of populations of *Aspergillus oryzae* (■) and *Penicillium chrysogenum* (◆) mycelia and mean projected area ( $A_p$ ).

branching behaviour of an organism by analysing the shape of the mycelial boundary would be highly advantageous in the study of more complex conformations where measures such as the hyphal growth unit are not readily obtainable. Furthermore, as has been demonstrated in other studies [6], [14], [16], [23], fractal analysis can be applied regardless of the gross morphological form that results in a particular process, allowing a more thorough compilation of data. However, a more complete analysis, including more complex structures, is necessary to validate the universal application of fractal analysis.

It has been previously suggested that the box-counting method of fractal dimension enumeration may not be suitable for the analysis of small, relatively unbranched hyphal structures [6], [24]. The accuracy of the box-counting method relies on an object being sufficiently great in size so as to allow a reasonably large variation in  $\epsilon$  (approximately one order of magnitude has been suggested [24]). Given a value of approximately  $4\mu\text{m}$  for  $\epsilon_{min}$  (hyphal width is approximately  $2\text{--}4\mu\text{m}$ ), this suggests a minimum value of approximately  $40\mu\text{m}$  for  $\epsilon_{max}$  in this study, equating to a minimum object ‘diameter’ of  $160\mu\text{m}$ . However, mycelia smaller than this dimension were often encountered, particularly in the case of *P. chrysogenum*. Further, the number of evaluations of  $N(\epsilon)$  is restricted by the image resolution (approximately  $1\mu\text{m}$  per pixel in this study). This can obviously be overcome by increasing the image resolution, but this in turn results in a significant increase in memory usage and processing time.

By enumerating the fractal dimension based on the object boundary, considerations of resolution are obviated to some degree, as the boundary can be represented geometrically as a series of equations, or indeed as a single spline, to be sampled as often as is necessary to provide sufficient signal resolution. However, image resolution is still an important consideration, as low-resolution images may not contain an accurate representation of the object boundary. Consideration must also be given to the means used to locate the boundary. In this study, hyphae were uniformly stained and object segmentation from background was accurately performed by grey-

scale thresholding. In cases where staining is non-uniform, thresholding may not be suitable and some form of edge-detection algorithm may be required.

While numerous studies have been conducted in which fractal analysis is utilised to quantify mycelial morphology, few have attempted to link fractal dimension with conventional morphological parameters. However, links have been established between fractal dimension and productivity in some processes. For example, in the optimisation of *Funalia trogii* fermentations, both fractal dimension and mean pellet area were monitored; while no link was established between the two parameters, it was suggested that a correlation may exist between fractal dimension and decolourisation of reactive black 5 [14]. A positive correlation was also found between fractal dimension and phenol-oxidase expression by *Pycnoporus cinnabarinus*, with both parameters being regulated by media composition [15].

Where links between fractal dimension and conventional Euclidean measures of morphology have been made, the relationship is often either ambiguous or qualitative in nature. An approximate correlation ( $R^2 = 0.614$ ) was found between the convexity (defined as the ratio between convex perimeter and respective perimeter) of *Cupriavidus necator* DSM 545 flocs and  $D_{BS}$  [28]. Fractal dimension was shown to be related to broth rheology in the submerged fermentation of *Cephalosporium acremonium* M25 and a relationship with other morphological measures, such as the number of arthrospores in the media, was also suggested, but not explicitly demonstrated [16]. A relationship between hyphal growth unit and fractal dimension of mycelia was previously noted in submerged fermentations of *Aspergillus niger*, but the differences in the recorded values of  $L_{HGU}$  were ambiguous [17]. Further studies of *A. niger* revealed that medium composition had a significant impact on the fractal dimension, the changes in morphology reflected in variations in the size and compactness of mycelial aggregates [6]. The local fractal dimension (determined by the concentric circles method) within a colony of *Trichoderma viride* was found to increase with branching frequency (occurrence of ‘loops’ in the mycelium), although the result was rather qualitative in nature [18]. However, successful attempts have been made in relating fractal dimension to growth kinetics. While colony expansion rates were found to differ between different strains of *Cryphonectria parasitica*, fractal dimension was found to correlate with the expansion rate, independent of strain [19].

#### IV. CONCLUSION

The optimisation of industrial fermentation processes involving filamentous microbes requires extensive knowledge of morphological development, as productivity is heavily influenced by the specific phenotypic form adopted by an organism in a certain process. The accurate quantification of morphological variation in vegetative mycelia is therefore of the utmost importance, but the characterisation of complex morphologies represents a significant challenge. The utility of conventional measures employed in the analysis of these microbes (such as projected area, perimeter length and circularity) is limited, as

they reveal little about the extent of branching of the organism, which is known to be related to metabolite production.

An alternative approach to morphological quantification employs the use of fractal geometry to characterise the spatial distribution of an organism. The self-similar nature of mycelial structures has been demonstrated in numerous studies and there is clearly significant potential benefit in the application of fractal analysis to filamentous microorganisms. What has been lacking in these studies is a firm link between fractal dimension and conventional morphological parameters, such as the hyphal growth unit. This study indicates a strong correlation between these two parameters in the analysis of 'free' mycelial elements and further investigation involving a wide range of complex conformations is necessary. Future work will focus on elucidating a universal relationship between fractal dimension, branching behaviour and productivity, independent of the gross morphological form encountered in a given process. It is hoped that this work will lead to a rapid and efficient means of morphological quantification for use in industrial processes.

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