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Predicting quality attributes of strawberry packed under modified atmosphere throughout the cold chain

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Abstract

Modified Atmosphere Packaging (MAP) is used commercially to extend the shelf life of strawberries. The attainment of desired gas (O₂, CO₂) concentrations inside MAP relies on the product respiration and the mass transfer through packaging and will affect the quality. The objective of this work is to build a mathematical model for strawberries to assess the effect of the uncertainties on headspace gas concentration and quality: 1) cold chain related temperature and relative humidity variations and 2) variability associated to product respiration and quality based on literature. Weight loss was more influenced by the cold chain storage conditions (temperature and RH) whereas spoilage had similar influence of cold chain conditions and product parameters. Waste generated in the cold chain was estimated from industrial standard weight loss and spoilage thresholds. A sensitivity analysis of the stochastic MAP model showed the influence of input parameters on the quality pointing to interventions associated to a reduction of the respiration rate (e.g. modification of packaging) and reduction of water transfer (e.g. coating) may prove more successful than other interventions to which the waste generation of this product is not so sensitive to. As a conclusion this work presents a
toolbox to interpret cold chain data: 1) develop mathematical models to predict fate of quality 2) simulate cold chain conditions allowing for uncertainty 3) estimate the waste generation kinetics based in quality criteria and thresholds 4) perform a sensitivity analysis to identify most sensitive technological parameters 5) identify interventions that will affect those technological parameters.

**Keywords:** mathematical modelling; coating, variability; sensitivity analysis; strawberry

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$a_w$</td>
<td>Water activity of fresh produce</td>
<td></td>
</tr>
<tr>
<td>$P_s$</td>
<td>Saturated vapour pressure</td>
<td>Pa</td>
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<tr>
<td>$A_c$</td>
<td>Surface area of produce (m$^2$)</td>
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<td>Film permeability to species (i = O$_2$, CO$_2$, H$_2$O) (mL m$^{-2}$ h$^{-1}$ atm$^{-1}$)</td>
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<td>Humidity Ratio</td>
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<td>Humidity Ratio of saturated water vapour</td>
<td></td>
</tr>
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<td>$K_a$</td>
<td>Air-film mass transfer coefficient (kg m$^{-2}$ s$^{-1}$ Pa$^{-1}$)</td>
<td></td>
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<tr>
<td>$K_s$</td>
<td>Skin mass transfer coefficient (kg m$^{-2}$ s$^{-1}$ Pa$^{-1}$)</td>
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<tr>
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<td>Michaelis-Menten constant in CO$_2$ evolution (% O$_2$)</td>
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<tr>
<td>$K mc_{CO_2}$</td>
<td>Michaelis-Menten constant for competitive inhibition of CO$_2$ (kPa)</td>
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<td>$K mc_{iO_2(f)}$</td>
<td>Michaelis-Menten constant for inhibition on the fermentative metabolism by (i = O$_2$, CO$_2$) (kPa)</td>
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<td>Respiratory Quotient</td>
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<td>$V_f$</td>
<td>Free volume in headspace (mL)</td>
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<tr>
<td>$V_{mO_2}$</td>
<td>Maximum O$_2$ consumption rate (mL kg$^{-1}$ h$^{-1}$)</td>
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</table>
1. Introduction

Strawberries are highly perishable in nature with high metabolic rate and thus have short shelf life. The major limiting factor of the quality of strawberries is spoilage due to *Botrytis* infection. The tissue of strawberry deteriorates through natural senescence during the food distribution chain and *Botrytis* develops due to tissue softening as a result of over ripening (Hertog et al., 1999). Other limiting factors to strawberry shelf
life are appearance, texture and taste, which are affected by decay and weight loss during the supply chain. The most effective intervention to extend the shelf life is to use low temperature storage (Sanz et al., 2000). Packaging is another important technique to extend the shelf life of perishable fruit to facilitate a longer transportation distribution (Caner et al., 2008). The storage quality can be further improved by using modified atmosphere packaging (MAP) and altering the concentration of gases surrounding the fresh strawberry (Geysen et al., 2005; Zhang et al., 2003).

MAP has been used to increase and preserve the shelf-life of produce, while also responding to the emerging consumer demand for convenience and quality. The design of optimal MAP for a specific produce depends on the characteristics of the produce, permeability of the packaging film and dependence on external factors such as temperature and relative humidity (Zagory and Kader, 1988). Apart from extending the shelf life of strawberries it maintains the quality characteristics firmness, prevents weight loss and microbial spoilage (Caner et al., 2008; Larsen and Watkins, 1995; Pelayo et al., 2003).

**Sources of uncertainty in postharvest distribution of strawberries**

Managing uniform quality of produce is a tedious task due to the many sources of variability, inherent biological variation and fluctuation occurring in storage conditions (Duret et al., 2015). Postharvest management aims at controlling the variation as much as possible by sorting and grading the product at different stages of the postharvest chain (Hertog et al., 2009a). Identifying and quantifying different sources of variance in the experimental data and assigning uncertainties to the parameter values and error provides better interpretation of the postharvest behaviour (Aguirre, 2008; Hertog et al., 2007a). Biological variation has been previously studied by including this variation in the quality change model, estimating the initial variation (“harvest age”) and using it to
assess the effect throughout the postharvest chain (Hertog et al., 2009b). Over the last decade models explaining biological variation in fresh produce have been developed (Duret et al., 2015; Gwanpua et al., 2014; Hertog et al., 2007b, 2004).

In a MAP gas exchange kinetic model the uncertainty can also be estimated at the respiration models of strawberries. Michaelis-Menten inhibition constants for O\textsubscript{2} consumption (\(Km_{O_2}\)) and fermentative CO\textsubscript{2} production (\(Kmc_{O_2}(f)\)), the reference rate constant of maximum oxygen consumption (\(Vm_{O_2}\)) and maximum carbon dioxide production (\(Vm_{CO_2}(f)\)) and the activation energy rate that have been experimentally assessed will have an associated uncertainty, conventionally in the form of a standard error (Hertog et al., 1999).

When describing the kinetics of weight loss in a packaged produce, the fruit skin mass transfer coefficient (\(K_s\)) is one of the main source of product variation due to the structural variation in the skin of individual fresh produce along with the initial spoilage of the batch (\(N_0\)) (Hertog et al., 1999). The statistical values of these parameters are presented in Table 2.

The objective of this study is to predict the quality of strawberry in the supply cold chain. The assessment of the effect of cold chain variability and product variability on the quality of strawberry will help estimate the waste generated. A sensitivity analysis was carried out to quantify the effect of different parameters and design an intervention that will reduce losses in the supply chain.

2. Materials and Methods

2.1. Model hypothesis

1. CO\textsubscript{2} production is a combination of oxidative and fermentative production, the oxidative consumption is proportional to the O\textsubscript{2} evolution and the fermentative production follows the Michaelis-Menten equations.
2. The temperature of the surface of commodity \( (T_s) \) is equal to the temperature of air surrounding the commodity \( (T_i) \).

3. The surface of the commodity is assumed to be perfectly saturated condition.

4. The metabolic energy released by produce, large part of it (80-100 \%) is dissipated as heat.

5. Condensation of water may occur in the product or the package when the free volume air relative humidity reaches 100\% using a saturated surface model.

6. The quality of strawberry is described as weight loss due to transpiration and by \( Botrytis \) spoilage as modelled by (Hertog et al., 1999).

2.2. Mathematical Model development

The mathematical model takes into account the heat and mass transfer balances due to the metabolic behaviour of strawberry and the transport phenomenon across package. The assumptions used in the mathematical model and sub model to describe respiration-transpiration of strawberry and gas transport across package (Table 1). The influence of these on the quality of strawberry during distribution chain is estimated.

2.2.1. Transpiration

Transpiration is caused due to vapour pressure deficit VPD (Pa) between the produce surface and the surrounding atmosphere (Xanthopoulos et al., 2012). VPD is the function of difference in the amount of moisture in air and the amount of moisture air can hold when it is saturated (Becker et al., 1996).

\[
VPD = (a_w - RH)p_s
\]  

1

It is assumed that water activity of strawberry is \( a_w \sim 0.99 \).
Saturated water vapour pressure at the surface of commodity can be calculated using following equation (Rennie and Tavoularis, 2009) based on saturated water vapour pressure data from ASHRAE (1997).

\[ p_s = 0.041081186T_s^3 - 32.431887T_s^2 + 8567.52691T_s - 757070.1 \]  

Transpiration occurs when water vapour pressure at the surface of commodity exceeds the water vapour pressure of the headspace of package (Becker et al., 1996; Xanthopoulos et al., 2012).

\[ m_w = VPD \times K_t \]

Transpiration rate (kg m\(^{-2}\)h\(^{-1}\)) is product of water vapour flux (\(m_w\)) and the surface area of the commodity (\(A_c\))

\[ t_r = m_w A_c \]

\[ K_t = \frac{1}{\left( \frac{1}{K_s} + \frac{1}{K_a} \right)} \]

Here, \(K_t\) is transpiration coefficient (kg m\(^{-2}\)s\(^{-1}\)Pa\(^{-1}\)) which is constant for the same commodity, \(K_s\) (kg m\(^{-2}\)s\(^{-1}\)Pa\(^{-1}\)) is skin mass transfer coefficient obtained from literature, \(K_a\) (kg m\(^{-2}\)s\(^{-1}\)Pa\(^{-1}\)) is air film mass transfer coefficient calculated using the Sherwood-Reynolds-Schmidt correlations (Becker et al., 1996).

\[ Sh = \frac{K_ad_c}{D_{H_2O,air}} \]

For convective mass transfer from commodity spherical in shape, (Becker et al., 1996) recommended Sherwood-Reynolds-Schmidt correlation of the following form to be used.

\[ Sh = 2.0 + 0.552 \ Re^{0.53} Sc^{0.33} = \frac{K_ad_c RT_s}{D_{H_2O,air} M_{H_2O}} \]
It is assumed, there is negligible flow around the commodity \((Re \approx 0)\). Therefore, air film mass transfer coefficient can be calculated as:

\[
K_a = 2 \times \frac{D_{H_2O-air} \cdot M_{H_2O}}{d \cdot R \cdot T_s}
\]

Transpiration Heat

The process of transpiration requires energy for evaporation of moisture from surface of produce, this process cools down the commodity. Evaporative heat transfer rate \((Q_{tr})\) is a product of latent heat of vaporization \((\lambda)\) and transpiration rate \((t_r)\).

\[
Q_{tr} = \lambda \cdot t_r
\]

2.2.2. Relative humidity in headspace

The concentration of water vapour inside the package is dependent on the rate of water vapour transfer from the moisture sources to moisture sinks within the package. The main moisture sources in the package is water transpired from the surface of fresh produce \((t_r)\) and the main source of moisture sink is permeation of water vapour through the film \((m_{pr})\) (Becker et al., 1996).

The amount of water vapour in the headspace is calculated using humidity ratio which is the ratio of mass of water vapour in headspace to mass of dry air in the headspace of package \((kg/kg)\).

\[
\frac{dHR}{dt} = \frac{t_r \cdot m_{pr}}{W_a}
\]

Relative humidity is calculated as ratio of humidity ratio inside the package \((HR)\) to the humidity ratio of saturated water vapour \((HR_{sat})\) (Jalali et al., 2017; Song et al., 2002).

\[
HR_{sat} = \frac{0.62198 P_s}{(P_{atm} - P_s)}
\]
In perforation mediated packaging condensation rate is seldom modelled in MAP, due to near saturation conditions and non-uniform or fluctuating temperature within the package, condensation can occur on the commodity surface or inside of package film and walls. It is assumed that the water vapour condensed on the surface of commodity does not penetrate the skin of fresh produce. For condensation to take place the partial pressure of water vapour should be greater than the saturated water vapour pressure (Jalali et al., 2017; Joshi et al., 2018; Rennie and Tavoularis, 2009).

\[
M_{con} = \begin{cases} 
K_a (P_{H_2O} - P_e) \delta A_c, & \text{if} (P_{H_2O} > P_s) \\
0, & \text{otherwise}
\end{cases}
\]

The corresponding rate of release of heat due to condensation on the surface of commodity is \( Q_{con} \) calculated as:

\[
Q_{con} = \lambda M_{con}
\]

The rate of condensation on package wall (\( M_{wcon} \)) is calculated similarly using air film mass transfer coefficient (\( K_a \)).

\[
M_{wcon} = \begin{cases} 
K_a (P_{H_2O} - P_s) \delta A_w, & \text{if} (P_{H_2O} > P_s) \\
0, & \text{otherwise}
\end{cases}
\]

The heat released during condensation (\( Q_{wcon} \)) heats up gases in atmosphere near wall.

\[
Q_{wcon} = \frac{\lambda M_{wcon}}{A_w}
\]

2.2.4. Quality

The quality of fresh produce is determined by the overall characteristics (appearance, texture, flavour and nutritive value) of fresh produce (ElMasry et al., 2007). The perception of quality is highly subjective and depends on consumer and number of
qualitative factors. Quality of fresh produce in general is often described using a chemical kinetic model (Merts, 1996). The main attributes of quality in strawberries is weight loss and spoilage.

2.2.4.1. Weight loss

The amount of water vapour transpired from the surface of fruit \( t_r \) and carbon loss due to respiration accounts for the weight loss.

\[
\frac{dW_t}{dt} = t_r + M_c r_{CO_2} W_s
\]  

2.2.4.2. Spoilage

The inhibition of spoilage in strawberry in modified atmosphere is assumed to be the result from inhibitory effect of gas composition on gas exchange in strawberry. When the gas exchange is inhibited the overall metabolic rate and the ripening rate will be inhibited resulting in a slower spoilage rate (Hertog et al., 1999). (Tijskens and Polderdijk, 1996) used relative metabolic rate (eq 18), which represents a ratio of the actual respiration rate under any gas conditions to the respiration rate under normal air conditions (21% \( O_2 \), 0.03% \( CO_2 \)) at the same temperature. In the case of strawberries fermentative activities are taken into account in the respiration model therefore the gas exchange is expressed in terms of \( CO_2 \) production.

\[
Rel_{MR} = \frac{r_{CO_2(t)}}{r_{CO_2(21\% O_2,0.03\%CO_2,T_0)}}
\]

The spoilage of strawberry due to \textit{Botrytis}, in terms of percentage of strawberry affected can be described by the following ordinary differential.

\[
\frac{dN}{dt} = Rel_{MR} \times k_s \times N \times \left( \frac{N_{max}-N}{N_{max}} \right), \text{ initiate at } N_0
\]
Where $N_{\text{max}}$ is maximum spoilage (100%), $k_s$ is the spoilage rate constant which depends on the temperature according to Arrhenius equation. The value of activation energy associated with the spoilage rate constant is mentioned in table 2.

2.3. Numerical Simulations of the ODE system

To estimate the effect of input parameter uncertainty on the prediction of concentration of gases and effect on quality during the cold chain distribution, Monte Carlo simulations were performed to simulate three scenarios:

1) A distribution scenario where temperature and relative humidity are varying with the cold chain data, as described in Joshi et al. (2018).

2) A distribution scenario with an ideal cold storage temperature (4°C) and relative humidity (80%) and with variable product properties, as specified in Table 6.2.

3) A distribution scenario considering the joint uncertainties of 1) and 2).

The value of product parameters used in the model are in table 2. The ordinary differential model was solved using the deSolve library (Soetaert et al., 2010) using the lsoda solver on R 3.4.3 (R Development Core Team, 2008). All the plots were produced using the ggplot2 library (Wickham, 2009). Sensitivity analysis using a main and first order interactive effects model excluding time were analysed using a Lowry plot (McNally et al., 2011).

2.4. Uncertainty assessment

2.4.1. Assessment of the impact of cold chain on quality in cold chain

A simulation scenario considering average product characteristics without variation and a variable cold chain temperature and relative humidity profile was used to assess the importance of different transport and retail conditions. This simulation scenario used cold chains of 3 and 6 days of temperature and relative humidity export profiles from (Joshi et al. 2018). The mathematical model was simulated against these
cold chain profiles to study the effect of cold chain uncertainty on the quality of strawberry results are presented in following sections

2.4.2. Assessment of product variability on waste production

A simulation scenario considering full product variability and constant storage conditions was used to assess the relative effect of different product variability sources. The storage conditions tested involved:

1) An ideal storage temperature of 4°C and relative humidity 80%.

2) An abuse cold chain composed of the following steps: 2 hours of packaging at 8°C followed by retail storage for up to 1.5 day at 4°C, transportation at 8°C for 1 day and retail shop storage at 4°C for 3 days.

The product parameters responsible for the variability are presented in Table 2.

The results in Section 2.6.2 shows the uncertainty due to the product parameters uncertainty on the quality parameters of strawberry.

To further investigate the effect of individual product parameter, a sensitivity analysis was performed using a main and first order interactive effects model excluding time. The results are presented using a Lowry plot (McNally et al., 2011)

2.4.3. Combined assessment of product and cold chain uncertainty effect on waste

Section 2.6.3 presents the combined assessment of cold chain uncertainty and product uncertainty. This study contributes to the identification of the relative influence of different parameter uncertainties and the interventions that can be designed to maintain the quality and reduce the waste in supply chain. A sensitivity analysis was also carried out to access the effect of individual parameters on the produce quality, as explained in the next section.

Sensitivity analysis
The input parameters of the sensitivity analysis are shown in Table 2. The results of the sensitivity analysis were presented using a Lowry plot (McNally et al., 2011). The total effect of the main parameters are given in black and any first order interactions with other parameters is represented in grey as a proportion of the variance. The ribbon represents the variance due to parameter interactions, while the cumulative sum of the main effects and the sum of the total effects is indicated by the lower line and upper line, respectively.

*Estimation of waste generation*

The losses observed in the strawberry cold supply chain are ascribed to weight loss and spoilage. The simulation results of product variability were used to calculate the waste generated based on the industrial thresholds. Conditional density plots were used to illustrate the waste produced in the strawberry supply chain.

2.5. Validation

Strawberry (150g, 3-5 cm diameter) were purchased from local wholesale fruit market Dublin, Ireland and packaged in an industry standard perforated polypropylene LDPE film (4 perforations) and were stored in either ideal conditions (4°C) or abuse condition (1/2 day in packaging facility at 8 °C followed by transportation at 4 °C up to 2 days, followed by retail storage including 4h at 20 °C, followed by 2 days at 8 °C, and finalised by retail shop 4h at 20°C 2 days at 8 °C) for a period of 10 days.

A chitosan solution (1.5 %) was prepared by dissolving chitosan (Sigma-Aldrich Ltd., UK, medium molecular weight, 75-85% deacetylated) in distilled water containing 1% glacial acetic acid using a magnetic stirrer. After complete dissolution 0.2% Tween 80 (Sigma-Aldrich Ltd., UK) was added to the solution. The pH of the solution was adjusted to 5.2 with 1N NaOH (Sigma-Aldrich Ltd., UK) (Petriccione et al., 2015). A second sample of the same batch of strawberries was immersed in chitosan solution for
60s then allowed to dry for 1 hour in air dryer at room temperature and stored in the same conditions as above.

Strawberries were visually examined on regular intervals during storage period. The fruits showed surface mycelia growth or bacterial lesions were considered decay. Results were expressed as percentage of spoiled fruits. Weight loss was expressed as percentage loss of initial weight (Han et al., 2004).

2.6. Results and discussions

2.6.1. Cold chain variability assessment

The mathematical model presented in section 2 was used to simulate the effect of cold chain variation on the changes in the concentration of gases in the headspace and quality of strawberry. The governing ODE equations (24 and 25) in table 1 were used to obtain the concentration of carbon dioxide and oxygen package’s headspace. The results presented in Fig 1 were simulated in contrast with the export cold chain. The creation and maintenance of optimal atmosphere inside the modified atmosphere package depends on the product’s respiration rate and on the permeability of the films, both of which are dependent on temperature. At very low oxygen concentration (<2%), anaerobic respiration is initiated in the tissue, which shortens the shelf life. However, the results obtained from the simulations showed there was no anaerobic condition was observed in the package.

Temperature fluctuations and their effect on the atmosphere inside the package had a major effect on strawberry quality. The spoilage increased with higher temperatures, however the effect of MA was also evident. A linear effect of CO$_2$ concentration on spoilage was. At 0% CO$_2$, 1.72 % spoilage was observed, versus to 0.87% spoilage at 18% CO$_2$ (Kader, 1986). At higher CO$_2$ concentration (20-80%), a clear inhibition occurred. At these extremely high levels of CO$_2$, fungal growth is indeed inhibited in
strawberries (Ke et al., 1991). The amount of water vapour in the headspace of the package was estimated using Fick’s diffusion and psychometric equations to calculate the relative humidity inside the package. The results showed that the package is saturated (RH=100%) during storage. Fishman et al. (1996) obtained similar results for MAP of mango, and Song et al. (2002) obtained similar experimental and predicted results of relative humidity saturating rapidly during storage.

Weight loss as a result of transpiration and carbon loss due to respiration was directly dependent on temperature (Fig 1 (c)). Sanz et al. (2000) reported weight loss of 3.53% in control packages and 0.9% in micro-perforated packages towards the end of storage (7 days). The barrier in the movement of water vapour through the film and perforations leads to less weight loss. The spike in spoilage (>5%) after 2 days of storage is attributed to the result of abusive temperature profile. A linear effect of CO₂ concentration was observed on spoilage: 1.72% spoilage at 0% CO₂ and 0.87% spoilage at 18% CO₂ (Kader, 1986).

2.6.2. Product variability assessment

Knowledge of the impact of biological variation on quality within a batch is very important to assure a uniform quality in the cold chain. Could the variability assessment aids the prediction of factors responsible for quality deterioration during storage. The model developed in this study can help find the effect of variability on the quality parameters. (Hertog et al., 1999). The results obtained are estimates of the values expected due to the variability in the product parameters. The dimensions used are shown in Table 2. Fig 3 shows the propagation of product parameters on the quality characteristics of strawberry at different storage temperatures (4, 8 and 20°C). It is evident from the figure that the variation is directly dependant on temperature, where the higher temperatures have higher associated variation.
V_m_{O_2,ref} and V_m_{CO_2(t),ref} are the respiration rate parameters which are directly dependant on temperature. The increase in temperature resulted in increase in the respiration rate. Geysen et al. (2005) reported the effect of temperature on the activation energy of maximum O_2 consumption. The weight loss of strawberry constantly increased with time and higher weight loss was observed at higher temperatures. Strawberries have no protective skin which leads to higher weight loss due to transpiration The uncertainty associated with weight loss due to the product parameters was lower. As the storage temperature increased, the variability also increased, as evident from Fig 3c. The weight loss was lower than 0.5% at 4°C in 10 days, whereas at 20°C the weight loss reached 2.7%. Spoilage increased with storage temperature, as shown in Fig 3d. Spoilage was lower than 15% in 10 days storage, around 37% at 8°C, 100% spoilage at 20°C in 6 days. The effect of CO_2 on spoilage could be explained by the effect of CO_2 on the respiration rate. Hertog and co-authors (1999) showed that Botrytis inoculated fruits displayed an inhibitory effect of CO_2 on spoilage levels below 20%, which was strongly batch dependant.

2.6.3. Comparing the effect of variability on strawberry quality

The uncertainty associated with cold chain variability (temperature and relative humidity) and the variation associated with biological product parameters were compared by plotting kernel density plots for each food chain distribution day and for each of the scenarios. Fig 3 (a) and (b) show how the concentration of gases in the package’s headspace is dependent both on cold chain and product variability. The second peak observed in the figure is the result of abusive storage temperature (>10°C). Variations at the 4th day of distribution in CO_2 and O_2 concentrations seems to be
largely cold chain dependent, however by day 6 the cold chain variation has reduced below the variation of the product.

The weight loss showed dependence on the cold chain factors and storage temperature and relative humidity. Strawberries stored at 1°C showed less than 1% weight loss in 8 days, versus 8% at 20°C in 4 days, which exceeds the acceptable limit (Nunes et al., 1998). The spoilage rate (Figure 5.4d) was most influenced by the cold chain factors at the start of storage, but product uncertainty had a more prominent impact later during storage. Strawberries have been found to be colonised by the fungus B. cinerea before packaging, with the fungal infection increasing with storage time and inadequate storage conditions (Almenar et al., 2007). The initial spoilage (N0) is a value representing initial ripening stage or sensitivity of strawberry to botrytis infection (Hertog et al., 1999).

From Fig 3c and Fig 3d it is evident that the cold chain conditions (temperature and relative humidity) need to be controlled in order to minimise the product’s weight loss. Nevertheless, in the case of spoilage the product parameters are the main cause of variability that need to be controlled to extend the shelf life.

2.6.4. Sensitivity Analysis

Sensitivity analysis was performed to study the results of variation and how it could be apportioned qualitatively and quantitatively to different sources of variation in the model input (Kader and Saltveit, 2003). The result of the sensitivity analysis (SA) on the weight loss of packed strawberry is presented in Fig 4 (a). The most important parameters contributing to the 90% of the variability were a combination of respiration rate parameters ($R_{Q,ox}, Vm_{O_2,ref}, K_{mO_2}$), skin mass transfer coefficient ($K_s$) and the activation energies associated with ($E_{avmO_2}, E_{avmCO_2(f)}$). Main effects interactive effects between the product parameters had an important impact on variability. This
result suggests that controlling the respiration rate of the fresh produce and reducing the mass transfer through their skin can help reduce losses during the supply chain.

*Identification of an effective intervention*

The sensitivity analysis of strawberry spoilage indicates that the most important parameters contributing to 90% of the variability are initial spoilage and spoilage rate constant ($k_{s,ref}$). Thus, the waste due to spoilage can be reduced by ensuring a good initial quality of strawberry and by controlling the spoilage rate during the supply chain. The product parameters contributing to the concentration of CO$_2$ in the package’s headspace were $Vm_{O_2,ref}$, $RQ_{ox}$ and $E_{Vm_{O_2,ref}}$. As these parameters contributed to 90% of the variability, a waste reduction would be achieved by controlling them.

2.6.5. Validation experiment

The input model parameters from Table 2 and 3 are used to compare the experimental and predicted results presented in the Fig 6. The experimental data comprises strawberry stored at ideal temperature (4°C) and abusive temperatures (4, 20, 8°C) for 10 days, in order to simulate real life supply chain conditions. Weight loss, colour, firmness and spoilage were measured at 1, 3, 5, 7 and 10 days. The grey ribbon represents the uncertainty margins of 5% and 95% percentiles ascribed to variability.

The results for weight loss showed that the variability associated with the product parameter is not high (Fig 5.3c). Cold chain parameters are responsible for the weight loss variability during the distribution chain of strawberry. Spoilage was highly variable and directly dependent on storage temperature (Fig. 5.3d). The experimental results fall within the uncertainty grey ribbon showing a good agreement with the prediction.
2.6.6. Waste generation estimation during the supply chain

Fig 6 shows the total waste estimation throughout the strawberry supply chain, as a combination of waste due to weight loss and spoilage. Threshold values were used to calculate the waste – weight loss ≥ 5%, when fruits start to shrivel and become unmarketable), and 5% spoilage. Significant amounts of out-of-specification product yielding to waste appear from day 2 of distribution; by the end of day 3, approximately 10% of all product would be potentially unsuitable for consumption, leading to waste generation.

2.7. Conclusions

A mathematical model was developed to predict the concentration of gases (O₂, CO₂) and water vapour in the packaging headspace. The model takes into account the heat and mass transfer processes occurring in MAP, such as respiration, transpiration condensation and transport of gases through the permeable film. The kinetic behaviour of fresh produce was modelled with respect to the cold chain conditions and product parameters. The effect of cold chain variability and product variability on the quality of fresh produce was assessed. Weight loss was shown to be influenced by the cold chain factors. In contrast, spoilage is initially impacted by the cold chain factors, but product variability becomes prominent towards the end of storage. The results of the sensitivity analysis showed that control of the respiration rate and skin mass transfer would help reduce the waste produced the during supply chain. The model validation showed that the model is a good fit to the experimental data.

3. Acknowledgement

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4. Bibliography


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J. Food Sci. 61, 956–961.


Han, C., Zhao, Y., Leonard, S.W., Traber, M.G., 2004. Edible coatings to improve storability and enhance nutritional value of fresh and frozen strawberries (Fragaria x ananassa) and raspberries (Rubus idaeus). Postharvest Biol. Technol. 33, 67–78.


Table 1 Equations used in the mathematical model

<table>
<thead>
<tr>
<th>Process</th>
<th>Equation</th>
<th>Reference</th>
<th>Eq. no.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Respiration</td>
<td>[ R_O_2 = \frac{v m_{O_2}}{K_{m_{O_2}}} \left(1 + \frac{</td>
<td>O_2</td>
<td>}{K_{m_{O_2}O_2}}\right) ]</td>
</tr>
<tr>
<td></td>
<td>[ r_{CO_2} = \frac{v m_{CO_2}}{K_{m_{CO_2}} +</td>
<td>CO_2</td>
<td>} ]</td>
</tr>
<tr>
<td></td>
<td>[ r_{CO_2} = R Q_{ox} \cdot r_{O_2} + r_{CO_2}(f) ]</td>
<td></td>
<td>22</td>
</tr>
<tr>
<td>Respiration heat</td>
<td>[ Q_S = \frac{2816}{6} \times \frac{r_{O_2} + r_{CO_2}}{2} \times \alpha \times W_p ]</td>
<td>(\alpha) is conversion factor of respiration energy dissipated as heat. The literature suggests the value of (\alpha) has a range between 0.8-1.0 (Burton, 1982). For 100% conversion of respiration energy as heat (\alpha = 1) (Song et al., 2002)</td>
<td>23</td>
</tr>
<tr>
<td>Mass Balance</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Permeability</td>
<td>[ \frac{d</td>
<td>O_2</td>
<td>}{dt} = 100 \times \left(\frac{A_p P_{O_2} \rho_{atm}}{L_f} \left</td>
</tr>
<tr>
<td></td>
<td>[ \frac{d</td>
<td>CO_2</td>
<td>}{dt} = 100 \times \left(\frac{A_p P_{CO_2} \rho_{atm}}{L_f} \left</td>
</tr>
<tr>
<td>Permeability</td>
<td>[ P_{O_2,CO_2,H_2O} = P_{O_2,CO_2,H_2O\text{ref}} + \frac{\pi R_h^2 \times D_{\text{air}}}{(L_f + R_h)} \times N_h ]</td>
<td>Permeability is a function of permeability of film and the number and size of perforations.</td>
<td>26</td>
</tr>
</tbody>
</table>
### Water permeation through film

\[
\frac{dm_{pr}}{dt} = \frac{P_{H_2O}A_p(P_t-P_o)}{L_f} \left[ 0.018P_{atm} \right]
\]

The driving force of permeation of water vapour from the headspace of package to surrounding is the water vapour pressure difference.

### Heat Balance

#### Temperature headspace of package

\[
\begin{align*}
Q_s W_s + Q_{con} + h_p A_p (T_i - T_o) &= Q_{tr} + W_s C_s \frac{dT_s}{dt} + W_a C_a \frac{dT_t}{dt} \\
\frac{dT_s}{dt} &= Q_r + Q_{con} - h_p A_p (T_i - T_o) - Q_{tr} \\
&= \frac{W_s C_s + W_a C_a}{W_s C_s + W_a C_a}
\end{align*}
\]

The heat is generated by respiration and heat is transferred in headspace due to convection, transpiration and condensation. This ODE is used to estimate the temperature of the fresh produce (Lee et al., 1996).
Table 2 Parameter estimate and their standard error for strawberry

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Standard error (SE)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$V m_{O_2,ref}$ ($\mu$mol kg$^{-1}$sec$^{-1}$)</td>
<td>0.27</td>
<td>0.010</td>
</tr>
<tr>
<td>$E_{avm_{O_2}}$ (J mol$^{-1}$)</td>
<td>74826</td>
<td>3451</td>
</tr>
<tr>
<td>$V m_{CO_2,(f),ref}$ ($\mu$mol kg$^{-1}$sec$^{-1}$)</td>
<td>0.50</td>
<td>0.22</td>
</tr>
<tr>
<td>$E_{avm_{CO_2,(f)}}$ (J mol$^{-1}$)</td>
<td>57374</td>
<td>14400</td>
</tr>
<tr>
<td>$K m_{O_2}$ (%)</td>
<td>2.63</td>
<td>0.274</td>
</tr>
<tr>
<td>$K m_{c_{CO_2}}$</td>
<td>$+\infty$</td>
<td>-</td>
</tr>
<tr>
<td>$K m_{u_{CO_2}}$</td>
<td>$+\infty$</td>
<td>-</td>
</tr>
<tr>
<td>$K m_{CO_2,(f)}$ (%)</td>
<td>0.056</td>
<td>0.041</td>
</tr>
<tr>
<td>$K m_{c_{CO_2,(f)}}$</td>
<td>$+\infty$</td>
<td>-</td>
</tr>
<tr>
<td>$K m_{CO_2,(f)}$ (%)</td>
<td>1</td>
<td>-</td>
</tr>
<tr>
<td>$K s$ ($k$g m$^{-2}$sec Pa)</td>
<td>$13.6 \times 10^{-9}$</td>
<td>4.8</td>
</tr>
<tr>
<td>$k_{s,ref}$ (day$^{-1}$)</td>
<td>0.60</td>
<td>0.045</td>
</tr>
<tr>
<td>$E a_s$ (J mol$^{-1}$)</td>
<td>70108</td>
<td>7056</td>
</tr>
<tr>
<td>$N_0$ (%)</td>
<td>0.83</td>
<td>0.10</td>
</tr>
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</table>

Table 3 Properties of packaging film, produce and other conditions used in the model

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P_{O_2,ref}$ (m$^3$m$^{-1}$h$^{-1}$m$^{-2}$Pa)</td>
<td>$8.5 \times 10^{-14}$</td>
<td>(Xanthopoulos et al., 2012)</td>
</tr>
<tr>
<td>$P_{CO_2,ref}$ (m$^3$m$^{-1}$h$^{-1}$m$^{-2}$Pa)</td>
<td>$2.8 \times 10^{-13}$</td>
<td>(Xanthopoulos et al., 2012)</td>
</tr>
<tr>
<td>$P_{H_2O,ref}$ (m$^3$m$^{-1}$h$^{-1}$m$^{-2}$Pa)</td>
<td>$4.5 \times 10^{-13}$</td>
<td>(Xanthopoulos et al., 2012)</td>
</tr>
<tr>
<td>$\rho_b$ (kg m$^{-3}$)</td>
<td>600</td>
<td>(Xanthopoulos et al., 2012)</td>
</tr>
<tr>
<td>$\epsilon$</td>
<td>0.27</td>
<td>(Xanthopoulos et al., 2012)</td>
</tr>
<tr>
<td>$\alpha_w$</td>
<td>0.99</td>
<td>(Xanthopoulos et al., 2012)</td>
</tr>
<tr>
<td>$C_s$ (kJ kg$^{-1}$ K$^{-1}$)</td>
<td>4</td>
<td>(ASHRAE, 2006)</td>
</tr>
<tr>
<td>$[CO_2]$ ($%$)</td>
<td>0.03</td>
<td>(Song et al., 2002)</td>
</tr>
<tr>
<td>$[O_2]$ ($%$)</td>
<td>21.0</td>
<td>(Song et al., 2002)</td>
</tr>
<tr>
<td>$M_{O_2}$ (kg mol$^{-1}$)</td>
<td>0.032</td>
<td>(Bird, 2002)</td>
</tr>
<tr>
<td>$M_{CO_2}$ (kg mol$^{-1}$)</td>
<td>0.044</td>
<td>(Bird, 2002)</td>
</tr>
<tr>
<td>$M_{H_2O}$ (kg mol$^{-1}$)</td>
<td>0.018</td>
<td>(Bird, 2002)</td>
</tr>
<tr>
<td>$R$ (J K$^{-1}$mol$^{-1}$)</td>
<td>8.314</td>
<td>(Bird, 2002)</td>
</tr>
<tr>
<td>$P_{atm}$ (Pa)</td>
<td>101325</td>
<td>(Bird, 2002)</td>
</tr>
<tr>
<td>$\rho_o$ (kg m$^{-3}$)</td>
<td>1.43</td>
<td>(Siracusa, 2012)</td>
</tr>
<tr>
<td>(\rho_{CO_2}(\text{kg m}^{-3}))</td>
<td>1.98</td>
<td>(Siracusa, 2012)</td>
</tr>
<tr>
<td>-----------------------------</td>
<td>------</td>
<td>--------------------</td>
</tr>
<tr>
<td>(T_{\text{ref}}(^{0}\text{C}))</td>
<td>10</td>
<td>(Hertog et al., 1999)</td>
</tr>
<tr>
<td>(N_H)</td>
<td>4</td>
<td>Experimental</td>
</tr>
<tr>
<td>(d_c(\text{m}))</td>
<td>0.03</td>
<td>Experimental</td>
</tr>
</tbody>
</table>

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Fig 1. Simulation results of average (a) oxygen concentration and (b) carbon dioxide concentration in the headspace of packages (c) weight loss observed and (d) spoilage against the cold chain profile.

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Fig 3 The effect of cold chain uncertainty (green) and product parameter uncertainty (orange) on the (a) oxygen concentration (b) carbon dioxide concentration in headspace (c) weight loss during storage (d) Spoilage of strawberry. Each subplot within (a), (b), (c) and (d) represents the simulated variation in a given distribution day.

Fig. 4 Lowry plot for the effect of product parameters on the a) weight loss b) spoilage, c) CO2

Fig. 5 Comparison of model predictions with the experimental data (points) at different storage conditions ((4, 8, 200 C) (a, b) and at ideal temperature (40C) (c,d) a) weight loss b) spoilage at (4, 8, 200 C) , c) weight loss and d) spoilage at (40C).

Fig. 6 Conditional density plot of total waste generated in the strawberry supply chain.
Fig 1. Simulation results of average (a) oxygen concentration and (b) carbon dioxide concentration in the headspace of packages (c) weight loss observed and (d) spoilage against the cold chain profile.
Fig 2 Propagation of product parameter variability observed in (a) concentration of oxygen (b) carbon dioxide in headspace (c) weight loss and (d) Spoilage observed in strawberry packed in modified atmosphere 15 days storage at 4°C and 80% RH with subplots showing 4, 8 and 20 perforations in the package.
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Fig. 4 Lowry plot for the effect of product parameters on the a) weight loss b) spoilage, c) CO$_2$
Fig 5 Comparison of model predictions with the experimental data (points) at abusive (a, b) and ideal storage conditions (c,d) a) weight loss b) spoilage at abusive, c) weight loss and d) spoilage at ideal for uncoated strawberries.
Fig. Conditional density plot for the estimation of total waste generated in a) uncoated and b) coated strawberries.